Submodular Batch Selection for Training Deep Neural Networks

K J Joseph, Vamshi Teja R, Krishnakant Singh, Vineeth N Balasubramanian
Indian Institute of Technology, Hyderabad
{cs17m18p100001,ee15btech11023,cs15mtech11007,vineethnb}@iith.ac.in

Abstract
Mini-batch gradient descent based methods are the de facto algorithms for training neural network architectures today. We introduce a mini-batch selection strategy based on submodular function maximization. Our novel submodular formulation captures the informativeness of each sample and diversity of the whole subset. We design an efficient, greedy algorithm which can give high-quality solutions to this NP-hard combinatorial optimization problem. Our extensive experiments on standard datasets show that the deep models trained using the proposed batch selection strategy provide better generalization than Stochastic Gradient Descent as well as a popular baseline sampling strategy across different learning rates, batch sizes, and distance metrics.

1 Introduction
Deep learning methods are currently the state-of-the-art machine learning models for many applications, including computer vision, language understanding, and speech processing. The standard method for training deep neural networks is mini-batch stochastic gradient descent (SGD) while using backpropagation to compute the gradients. The mini-batch SGD is an optimization algorithm where mini-batches of data \( D_t = \{d_1, d_2, \ldots, d_m\} \) containing \( m \) examples are sampled uniformly from the dataset \( D \), at time \( t \). A loss function value w.r.t. the current model parameters \( w_t \) is computed as \( L(w_t) = \sum_{i=1}^{m} l(d_i|w_t) \) (where \( l(.) \) is any differentiable loss function for the neural network), and the weights are updated to minimize \( L(w_t) \), according to the following equation:

\[
    w_{t+1} = w_t - \mu_t \frac{\partial L(w_t)}{\partial w_t}
\]

where \( \mu_t \) is the learning rate at the \( t^{th} \) step.

In this work, we hypothesize and validate that not only is the update of \( w_t \) given \( \frac{\partial L(w_t)}{\partial w_t} \) crucial, but also the selection of the mini-batch \( D_t \) used to compute the gradient. We formulate batch selection as solving a submodular optimization problem, which contributes to significant improvement in the generalization performance of the model. To the best of our knowledge, this is the first such effort on submodular importance sampling for SGD.

Each mini-batch selection is posed as a cardinality-constrained monotone submodular function maximization problem. This helps us leverage a greedy algorithm to solve this NP-hard combinatorial optimization problem, which guarantees a solution for a submodular objective function which is at least (in the worst case) \( (1 - \frac{1}{e}) \) (approximately 0.63) of the optimal solution [Nemhauser et al., 1978].

The key contribution of our work is a new submodular sampling strategy for mini-batch SGD, which helps train deep neural networks to have better generalization capability. To achieve this, we formulate a submodular objective function, which takes into account the informativeness that each sample can add to the subset and at the same time ensure that the subset as a whole, is diverse. Further, we propose an efficient algorithm to scale to high sampling rates, as required for SGD while training neural networks. We conduct extensive experimental studies of the proposed submodular mini-batch selection methodology and show that it improves generalization capability of SGD as well as related previous efforts such as Loss based sampling [Loshchilov and Hutter, 2015]. We also show that the improved performance of the proposed methodology is consistent across different learning rates, mini-batch sizes and distance metrics. While submodular batch selection has been used extensively in the past for other settings such as active learning [Wei et al., 2015; Chakraborty et al., 2015] and other methods such as Determinantal Point Process (DPP) [Zhang et al., 2017] have been used to diversify minibatch selection recently, to the best of our knowledge, this is the first submodular batch selection methodology for SGD while training neural networks. Importantly, our consistent increase in generalization performance over SGD is a notable achievement, which was missing in methods proposed earlier for mini-batch selection. We use the terms batch selection and mini-batch selection interchangeably in this work.

The remainder of this paper is organized as follows. We survey the literature related to our work in Section 2; introduce our submodular function and describe our efficient implementation strategy in Section 3. The end-to-end algorithm is summarized in section 3.3. The experimental setup, main results, and ablation studies are reported in Section 4. We conclude in Section 5.
2 Related Work

Mini-batch selection strategies have been explored in convex settings in the past. [Zhao and Zhang, 2014] proposed a sampling scheme based on partitioning data into balanced strata leading to faster convergence, while [Zhao and Zhang, 2015] proved that the optimal sampling distribution is directly related to the absolute values of the gradient of the samples for convex objectives. However, the prohibitive cost of evaluating the gradient impedes their usage in practice. In non-convex settings, such as in deep neural networks, there have been fewer efforts for mini-batch selection, especially in the context of SGD. Extensions of [Zhao and Zhang, 2015] to neural networks do not scale, due to the large number of trainable parameters in the deep models. Recently, [Loschilov and Hutter, 2015; Alain et al., 2015] have tried to alleviate the cost of computing gradients by using loss-based sampling as an approximation to the gradients. Unfortunately, these methods are very sensitive to hyperparameters and perform inadequately in many cases [Katharopoulos and Fleuret, 2017]. The work was, in fact, validated only on MNIST data, which was acknowledged as a limitation of the work in [Loschilov and Hutter, 2015]. The only other efforts to our knowledge consider more efficient approximations to the batch gradients i.e. variance of the samples [Chang et al., 2017] or an upper bound on the gradient norm [Katharopoulos and Fleuret, 2018], but the generalization performance is only comparable to SGD in most cases. On the other hand, there have been efforts to speed up mini-batch SGD in general such as [Allen-Zhu, 2017; Johnson and Zhang, 2013]. However, these efforts do not focus on batch selection or importance sampling, and show lower performance than existing importance sampling methods as noted in [Katharopoulos and Fleuret, 2018].

Submodular optimization has been successfully applied to varied tasks like document summarization [Lin and Bilmes, 2011], speech recognition systems [Wei et al., 2014], to name a few. However, there has been no work so far on using submodularity for batch selection. [Das and Kempe, 2008] proved that variance between a predictor variable using full batch and a mini-batch is submodular. We were initially motivated by this observation to propose a submodular batch selection strategy for SGD. The existing efforts that are closest to ours include Determinantal Point Process (DPP) [Zhang et al., 2017], Repulsive Point Processes (RPP) [Zhang et al., 2018] and [Singh and Balasubramanian, 2018]. Both DPP and RPP can be considered a special case of probabilistic submodular functions (PSF), although not explicitly called so in their work. However, these methods are computationally inefficient. Even with faster versions, they are prohibitively costly to be applied in deep neural networks [Li et al., 2016]. [Singh and Balasubramanian, 2018] attempt a similar objective, but the objective considered is truly not submodular, and their results are largely inconclusive. Another body of work that can be considered close to our efforts are those of self-paced learning [Thangarasa and Taylor, 2018] and curriculum learning [Zhou and Bilmes, 2018]. However, their objectives are different, and one can consider using our batch selection strategy along with any such method too.

3 Methodology

3.1 Submodular Batch Selection

An appropriate batch selection strategy for mini-batch SGD would need to consider multiple criteria to choose the most relevant samples. A primary criterion we consider is that each selected sample must be as informative as possible. We use the model uncertainty as the measure of informativeness.

Uncertainty Score \( U(x_i) \)

The uncertainty of each data point is computed as the entropy of the current model \( w^t \) at training iteration \( t \). \( C \) is the set of all classes. This allows the model to select the samples that confuses it the most in a mini-batch:

\[
U(x_i) = -\sum_{y \in C} P(y|x_i, w^t) \log P(y|x_i, w^t) \tag{2}
\]

A subset that maximizes only the Uncertainty Score, would potentially lead to the inclusion of similar data points with high entropy in the mini-batch. This redundancy should be avoided to make the mini-batch diverse. The following score helps to contain the inclusion of redundant data points:

Redundancy Score \( R(x_i) \)

Two data points \( x_i \) and \( x_j \) may separately furnish valuable information, but including both may make the subset less maximally informative. We use Redundancy Score to take this into account. Given \( \phi(.) \) to be any distance metric between the two data points, a greater value of the minimum distance between points in the subset would imply more diversity among the data points in the subset. (Needless to say, this score is dependent on the choice of distance metric, and we study this in our experiments.)

\[
R(x_i) = \min_{x_j \in S: i \neq j} \phi(x_i, x_j) \tag{3}
\]

Going further, one can notice that outlier samples may maximize the above scores. In order to counter such a selection of batches, we introduce the following score:

Mean Closeness Score \( MC(x_i) \)

This term encourages the selection of data points that are closer to the mean of all the examples (\( \mu = \frac{1}{|S|} \sum_{k=1}^{|S|} x_k \)) to be picked. This avoids the selection of outlier samples to the extent possible.

\[
MC(x_i) = \phi(x_i, \mu) \tag{4}
\]

Finally, there has been recent work to show that closeness in the feature space of a deep neural network may be a better indicator of how similar two samples are (as shown by [Wei et al., 2014] in the speech domain). We hence also include a term to explicitly enforce diversity in the feature space of the given data.

Feature Match Score \( FM(x_i) \)

This score selects samples that are diverse across each dimension in the feature space. \( g(.) \) is a non-negative monotone non-decreasing concave function, \( U \) is a set of fixed features.
and $m_u(x_i)$ is a non-negative score, measuring the degree to which data point $x_i$ possesses the feature $u$.

\[
FM(x_i) = \sum_{u \in U} g(m_u(x_i)) \tag{5}
\]

Our implementation of this score (as well as others) is described in Section 4.1.

We combine the above-mentioned scores to form our objective function for batch selection, $\mathcal{F}(S)$, as below and then show the submodularity of the proposed $\mathcal{F}(S)$.

\[
\mathcal{F}(S) = \sum_{x_i \in S} \lambda_1 U(x_i) + \lambda_2 R(x_i) + \lambda_3 MC(x_i) + \lambda_4 FM(x_i)
\]

Given a dataset with $N$ training data points, a mini-batch of size $k$ is selected by solving the following cardinality-constrained submodular optimization problem:

\[
\max_{S \subseteq V, |S| \leq k} \mathcal{F}(S) \tag{7}
\]

We now show that the score function $\mathcal{F}$ is indeed submodular and is monotonically non-decreasing. This would allow us to solve the problem in (7) using a greedy approach [Nemhauser et al., 1978].

**Lemma 1.** The score function $\mathcal{F}(\cdot)$, defined in Eqn 6 is submodular.

**Proof.** Consider two subsets of training examples from a dataset $V = \{x_1, x_2, \ldots, x_N\}$; $S_1$ and $S_2$, such that $S_1 \subseteq S_2 \subseteq V$. Let $a$ be an element not selected so far: $a \in V \setminus S_2$. The marginal gain of adding $a$ to $S_1$ is given by:

\[
\mathcal{F}(a|S_1) = \mathcal{F}([a] \cup S_1) - \mathcal{F}(S_1)
\]

\[
= \lambda_1 U(a) + \lambda_2 \min_{a_j \in S_1} \phi(a, a_j) + \lambda_3 MD(a) + \lambda_4 FM(a)
\]

Similarly, the marginal gain of adding $a$ to $S_2$ is given by:

\[
\mathcal{F}(a|S_2) = \mathcal{F}([a] \cup S_2) - \mathcal{F}(S_2)
\]

\[
= \lambda_1 U(a) + \lambda_2 \min_{a_j \in S_2} \phi(a, a_j) + \lambda_3 MD(a) + \lambda_4 FM(a)
\]

Since $S_1 \subseteq S_2$, the minimum distance of the new point $a$, from $S_1$ would be greater than any element from $S_2$, as there may exist a point in $S_2$ that is much closer to $a$, than any element from its subset $S_1$. Hence,

\[
\min_{a_j \in S_1} \phi(a, a_j) \geq \min_{a_j \in S_2} \phi(a, a_j)
\]

Thus, we can claim $\mathcal{F}(a|S_1) \geq \mathcal{F}(a|S_2)$. Hence, the score function $\mathcal{F}(\cdot)$ is submodular.

**Lemma 2.** The score function $\mathcal{F}(\cdot)$ in Eqn 6 is a monotonically non-decreasing function.

**Proof.** Consider a subset $S$ and an element $a \in V \setminus S$. When $a$ is added to $S$, the function value of $\mathcal{F}([a] \cup S)$ changes by $\lambda_1 U(a) + \lambda_2 \min_{a_j \in S} \phi(a, a_j) + \lambda_3 MD(a) + \lambda_4 FM(a)$. All these are non-negative quantities. Thus, $\mathcal{F}([a] \cup S) \geq \mathcal{F}(S)$, and the score function $\mathcal{F}(\cdot)$ is hence monotonically non-decreasing.

**Theorem 1.** Let $S^*$ denote the optimal solution of the problem in (7) and $S$ denote the solution obtained for the same problem using a greedy approach. Then:

\[
\mathcal{F}(S) \geq (1 - \frac{1}{e})\mathcal{F}(S^*)
\]

**Proof.** Having proved that score function $\mathcal{F}(\cdot)$ is submodular in Lemma 1 and that it is monotonically non-decreasing in Lemma 2, the proof follows directly from Theorem 4.3 in [Nemhauser et al., 1978].

### 3.2 Scaling to High Sampling Rates

It is interesting to note that application settings where submodularity has worked well hitherto [Wei et al., 2014; 2015; Chakraborty et al., 2015; Lin and Bilmes, 2011] do not require a high sampling rate, as much as demanded by mini-batch selection in SGD. Consider a mini-batch training algorithm that consists of $p$ epochs and $q$ iterations in each epoch, the submodular batch selection needs to be carried out $p \times q$ times. Concretely, for training on the CIFAR-100 dataset having 50,000 examples and a batch size of 50 ($q$ is hence 50000 / 50), we need 100,000 batch selections for 100 epochs ($p = 100$). Even a greedy algorithm [Nemhauser et al., 1978] that uses scores such as pairwise distance metrics has a complexity of $O(n^2)$, where $n$ is the dataset size. This would be too slow for use with SGD. We hence seek more efficient mechanisms to implement the proposed batch selection strategy.

Recent efforts have attempted to make submodular sampling faster in a more general context (not in SGD), such as Lazy Greedy [Minoux, 1978], Lazier than Lazy Greedy (LtLG) [MizraSOLEIMAN et al., 2015], and Distributed Submodular Maximization [MizraSOLEIMAN et al., 2013]. In this work, we present a new methodology for efficient submodular sampling inspired by Distributed Submodular Maximization algorithm and Lazier than Lazy Greedy algorithm (LtLG), as described in Algorithm 1. The algorithm partitions the training set $V$ into $m$ partitions in Line 2 and runs Lazier than Lazy Greedy algorithm (LtLG) [MizraSOLEIMAN et al., 2015] (described later in this section) on each partition (Lines 5 through 8) to obtain $m$ subsets, each of size $b$. These subsets ($S_i$s) are then merged in Line 9. The final subset $S$ is selected from this merged set by running LtLG again on it. This divide-and-conquer strategy is motivated by the Distributed Submodular Maximization algorithm [MizraSOLEIMAN et al., 2013].

The Lazier than Lazy Greedy (LtLG) [MizraSOLEIMAN et al., 2015] algorithm starts with an empty set and adds an element from set $R$, which maximizes the marginal gain $\mathcal{F}(a|S) = \mathcal{F}(a\cup S) - \mathcal{F}(S)$. This is repeated until the cardinality constraint ($|S| \leq b$) is met. The set $R$ is created by randomly sampling $s = \lceil \sqrt{\frac{k}{b}} \log \frac{1}{\epsilon_c} \rceil$ items from the superset $V$, where $\epsilon_c$ is a user-defined tolerance level. We refer the readers to [MizraSOLEIMAN et al., 2015] for further information. The model at the $k^{th}$ training iteration, $w_k$, is used while computing $\mathcal{F}(\cdot)$ as defined in Equation 6. The solution produced by Algorithm 1, $S$, has the following approximation guarantee.
Algorithm 1 Algorithm GetMiniBatch

Input: Training set $V$, Model at $k^{th}$ iteration $w_k$, Batch size $b$, Number of partitions $m$, $F : 2^V \rightarrow \mathbb{R}$ (Eqn 6).

Output: Mini-batch $S \subseteq V$ satisfying $|S| \leq b$.

1: $S \leftarrow \phi$
2: Partition $V$ into $m$ sets $V_1, V_2, V_3, \cdots, V_m$.
3: for $i = 1$ to $m$ do
4: \hspace{1em} $S_i \leftarrow \phi$
5: \hspace{2em} for $j = 1$ to $b$ do \hspace{1em} \hspace{1em} $\triangleright$ Do LILG for each partition.
6: \hspace{3em} $R \leftarrow$ a subset of size $s$ obtained by sampling randomly from $V_i \setminus S_i$.
7: \hspace{4em} $a_j \leftarrow \arg\max_{a \in R} F(a|S_i)$
8: \hspace{5em} $S_i \leftarrow S_i \cup \{a_j\}$
9: \hspace{2em} $S_{merged} \leftarrow \bigcup_{i=1}^m S_i$ \hspace{1em} \hspace{1em} $\triangleright$ Merge result of each partition.
10: \hspace{3em} for $j = 1$ to $b$ do \hspace{1em} \hspace{1em} $\triangleright$ Do LILG on the merged set.
11: \hspace{4em} $R \leftarrow$ a subset of size $s$ obtained by sampling randomly from $S_{merged} \setminus S_i$.
12: \hspace{5em} $a_j \leftarrow \arg\max_{a \in R} F(a|S)$
13: \hspace{6em} $S \leftarrow S \cup \{a_j\}$
14: Return $S$

with the optimal solution $S^*$:

$$F(S) \geq \frac{(1 - e^{-1})^2}{\min(m, b)} (1 - e^{-1} - e) F(S^*) \quad (8)$$

Here, $m$ refers to the number of partitions, $b$ refers to the mini-batch size and $e$ is the base of natural logarithm. Our empirical results (Section 4.2) shows that the approximation is much better than this lower bound in practice.

3.3 Gradient Descent with Submodular Batches

The proposed batch selection strategy can work with any mini-batch gradient descent based optimization algorithms. Algorithm 2 summarizes the end-to-end training procedure.

Algorithm 2 Algorithm Submodular SGD

Input: Training Set $V$, Optimizer $\pi(., \eta)$, # of epochs $p$, Batch size $b$, # of partitions $m$.

Output: Trained model $w_{\nu^+}$.

1: $\tau \leftarrow 1$
2: Initialize the model $w_1$
3: for $i = 1$ to $p$ do
4: \hspace{1em} for $j = 1$ to $|V|$ do
5: \hspace{2em} $S \leftarrow \text{GetMiniBatch}(V, w_j, b, m)$
6: \hspace{3em} $\nabla J(w_j) \leftarrow \frac{\partial}{\partial w_j} \sum_{k \in S} L(y_k, f(x_k, w_j))$
7: \hspace{4em} $w_{\nu^+} \leftarrow w_{\nu^-} + \pi(\{w_{\nu^+}\}, \{\nabla J_{\nu^+}\}, \eta)$
8: \hspace{5em} $w_{\nu^+} \leftarrow w_{\nu^+}; \tau \leftarrow \tau + 1$
9: return $w_{\nu^+}$

Within each iteration in each epoch, a mini-batch $S$ is selected using Algorithm 1 (Line 5). Lines 6 and 7 update $w$ with a gradient descent optimizer $\pi(., \eta)$, consuming the current set $S$. $\eta$ is the learning rate. Any differentiable loss function can be used as $L(.)$. Momentum-based and adaptive learning rate-based gradient descent methods could be used to further improve the learning based on submodular batches.

4 Experiments and Results

We conduct extensive experimental evaluations to study the effectiveness of submodular mini-batches in training deep neural networks over Stochastic Gradient Descent (SGD) and Loss-based sampling [Loshchilov and Hutter, 2015], as in earlier efforts such as [Katharopoulos and Fleuret, 2018]. For brevity, we refer to our proposed method of selecting submodular mini-batches for training as SubModular Data Loader (SMDL). We study the performance on the standard image classification task (as used in related earlier efforts) with SVHN [Netzer et al., 2011], CIFAR-10 and CIFAR-100 [Krizhevsky and Hinton, 2009] datasets. ResNet 20 [He et al., 2016] is used as the network architecture for SVHN and CIFAR-10, while ResNet 32 is used with CIFAR-100. Our implementation details are described in Sec 4.1, followed by the main result and various ablation study results in Sec 4.2.

4.1 Implementation Details

Algorithm 2 gives the generalized training procedure for submodular mini-batch selection. In each iteration, the current model $w_\nu^-$ is used to evaluate the submodular objective score (Equation 6). The feature representation for the images is obtained from the penultimate fully connected layer of this model. The probability values ($P(y|x_i, w)$) that are used in the computation of Uncertainty Score is the softmax output from the model. Euclidean distance between the image features is used for Redundancy Score computation in Equation 3. We do an ablation study on the effect of using other distance metrics in Section 4.3. Mean Closeness Score is computed as the cosine similarity between each data-point and the mean of all the training examples.

We follow the method used in [Brahma and Othon, 2018] and [Zhou and Bilmes, 2018] to compute the fixed feature set $U$ used for evaluating Feature Match Score (Equation 5). We train a corresponding neural network, say $M$, on a random subset of training data, for an epoch. The features from the penultimate fully connected layer of $M$ is used as $U$. Square root function is used as $g(.)$. $m_u(x_i)$ is the feature at $u$th index of the representation of $x_i$ from the model $M$.

After a grid search and an empirical study, we use the following values for the co-efficients of the terms in the objective function: $\lambda_1 = 0.2, \lambda_2 = 0.1, \lambda_3 = 0.5, \lambda_4 = 0.2$. Ablation studies of the effect of the $\lambda$ parameters are presented in Section 4.3. Each of the scores is individually normalized across the selected pool of samples, before being combined, to ensure fair comparison. All the score computation (which depends on the softmax output and the feature representation from fully-connected layers) is a function of the model at each iteration (Line 5, Algorithm 2). As we are using gradient descent for updating the parameters, we know that the model does not change drastically between iterations. Computational efficiency can be improved if we share the same model between successive iterations. We use a refresh rate of 5 for all the experiments. A study of how our method behaves with different refresh rates is shown in Figure 2(d).
that increasing the refresh rate decreases the performance of the model. This is because the model changes over multiple iterations, which in turn affects the quality of the mini-batch selected.

We develop a modularized and configuration-driven tool in PyTorch [Paszke et al., 2017], which implements submodular selection and the other two baseline methods: SGD and Loss based sampling [Loshchilov and Hutter, 2015]. All the experiments are run for 100 epochs with a batch size of 50, a momentum parameter of 0.9 and weight decay of 0.0001. Use of batch normalization [Ioffe and Szegedy, 2015] and adaptive learning methods like Adam [Kingma and Ba, 2014] will complement the reported results of SMDL and other baseline methods. For SGD, all the reported results are the average of five runs. The partition size (m in Algorithm 1 and 2) is set to 10. Source code and supplementary material which includes additional results is available here: https://josephkj.in/projects/SMDL

4.2 Results

We present the major result of our proposed submodular mini-batch selection method, SMDL in Figure 1 and Table 1. We train the two network architectures on three datasets as enumerated in Section 4. The generalization performance of these classification models, as measured by their test accuracy and test loss, is used as the evaluation metric. We see from Figure 1 and Table 1 that SMDL is able to achieve lower error and loss, consistently across epochs, on all the three datasets. It is worth noting that Loss-based sampling fails significantly on SVHN. Such deterioration of generalization performance is also noted in [Loshchilov and Hutter, 2015]. The values reported on SGD are its mean after conducting five trials. These results support our claim that selecting a mini-batch which respects diversity and informativeness of the samples helps in more generalizable deep learning models.

4.3 Ablation Studies

Effect of Trade-off Parameters

We study the effect of trade-off parameters that control the contribution of each of the four score functions in the submodular objective function (Equation 6). For this, we train ResNet 20 on a small subset of SVHN dataset. Except for

<table>
<thead>
<tr>
<th>Dataset</th>
<th>Method</th>
<th>Accuracy</th>
<th>Loss</th>
</tr>
</thead>
<tbody>
<tr>
<td>SVHN</td>
<td>Loss Based</td>
<td>90.87</td>
<td>0.363</td>
</tr>
<tr>
<td></td>
<td>SGD</td>
<td>93.60</td>
<td>0.230</td>
</tr>
<tr>
<td></td>
<td>SMDL</td>
<td>95.46</td>
<td>0.175</td>
</tr>
<tr>
<td>CIFAR-10</td>
<td>Loss Based</td>
<td>81.06</td>
<td>0.590</td>
</tr>
<tr>
<td></td>
<td>SGD</td>
<td>82.54</td>
<td>0.535</td>
</tr>
<tr>
<td></td>
<td>SMDL</td>
<td>84.85</td>
<td>0.487</td>
</tr>
<tr>
<td>CIFAR-100</td>
<td>Loss Based</td>
<td>53.77</td>
<td>1.755</td>
</tr>
<tr>
<td></td>
<td>SGD</td>
<td>53.37</td>
<td>1.764</td>
</tr>
<tr>
<td></td>
<td>SMDL</td>
<td>57.23</td>
<td>1.717</td>
</tr>
</tbody>
</table>

Table 1: Quantitative comparison of the proposed SMDL with SGD and Loss based sampling scheme on SVHN, CIFAR-10 and CIFAR-100 datasets. Mean refers to the mean accuracy(%) across epochs and Final refers to the final accuracy.
In this work, we cast the selection of diverse and informative mini-batches for training a deep learning model as a submodular optimization problem. We design a novel submodular objective and propose a scalable algorithm to do submodular selection. Extensive experimental valuation on three datasets reveals significant improvement in convergence and generalization performance of the model trained with submodular mini-batches over SGD and Loss based sampling [Loschilov and Hutter, 2015]. The ablation results show that the method is robust to changes in batch size and learning rate.

5 Conclusion

Acknowledgements

We would like to thank MHRD, Govt of India for funding the personnel involved, Microsoft Research India and ACM-India/IARCS for the travel grants to present the work and the anonymous reviewers for their valuable feedback.
References


