

Learning Concise Representations of Users’ Influences through Online Behaviors

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Abstract

Whereas it is well known that social network users influence each other, a fundamental problem in influence maximization, opinion formation and viral marketing is that users’ influences are difficult to quantify. Previous work has directly defined an independent model parameter to capture the interpersonal influence between each pair of users. However, such models do not consider how influences depend on each other if they originate from the same user or if they act on the same user. To do so, these models need a parameter for each pair of users, which results in high-dimensional models becoming easily trapped into the overfitting problem. Given these problems, another way of defining the parameters is needed to consider the dependencies. Thus we propose a model that defines parameters for every user with a latent influence vector and a susceptibility vector. Such low-dimensional and distributed representations naturally cause the interpersonal influences involving the same user to be coupled with each other, thus reducing the model’s complexity. Additionally, the model can easily consider the sentimental polarities of users’ messages and how sentiment affects users’ influences. In this study, we conduct extensive experiments on real Microblog data, showing that our model with distributed representations achieves better accuracy than the state-of-the-art and pair-wise models, and that learning influences on sentiments benefit performance.

1 Introduction

Social network services generally allow users to post, forward, share, or “like” a piece of information; to comment on a product or service; or to “check in” at a place of interest. All the above behaviors can be grouped as temporal sequences of users’ activity, which are known as temporal cascades. Thus a temporal cascade contains users’ actions with regard to a specific piece of information, product, place, etc. Since such actions are publicly visible, and since the system purposefully shares the information with related users or communities,

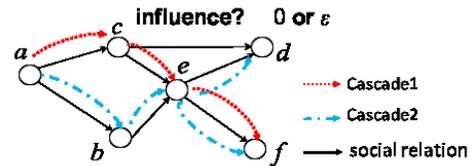


Figure 1: Previous pair-wise work gave an overfitting influence to (c, d)

users in a cascade influence each other [Goyal *et al.*, 2010; Althoff *et al.*, 2016], similar to a contagion of behaviors.

Scholars have applied the concept of contagion to study viral marketing [Richardson and Domingos, 2002], influence maximization [Gionis *et al.*, 2013; Du *et al.*, 2016b; Lu *et al.*, 2016], and how opinion forms [Bindel *et al.*, 2015; Wang *et al.*, 2016a]. These studies and applications need a way to know the causality of who influences whom, as well as accurate values of influences. In addition, the influences are usually different, depending on who the actors and recipients of the action are [Aral and Walker, 2012]. Therefore, accurately quantifying the interpersonal influences involved is fundamental to a proper understanding of viral marketing, influence maximization, and understanding opinion formation.

In previous works, interpersonal influences are estimated by machine learning from the observed data [Saito *et al.*, 2008]. Those studies suffer from the overfitting problem in sparse data, because of how they define their model parameters. A free parameter on each user pair in those models. Such pair-wise parameters do not consider dependency, especially when those influences originate from or act on the same user. For the parameters of such user pairs, the overfitting problem occurs, resulting in inaccurate estimation. For an intuitive example in Figure 1, the interpersonal influence cannot be learned for user pair c and d, who do not appear in the same cascade with information passing between them. In such a case, even though c, d, and e form a social triangle, a zero or some empirically small constant ϵ is assigned, implying that information would never or seldom be passed between them in the future, which can be inaccurate. In fact, power-law-like distributions can always be found in social network analysis, which suggests that the number of user pairs between whom information is rarely passed cannot be ignored.

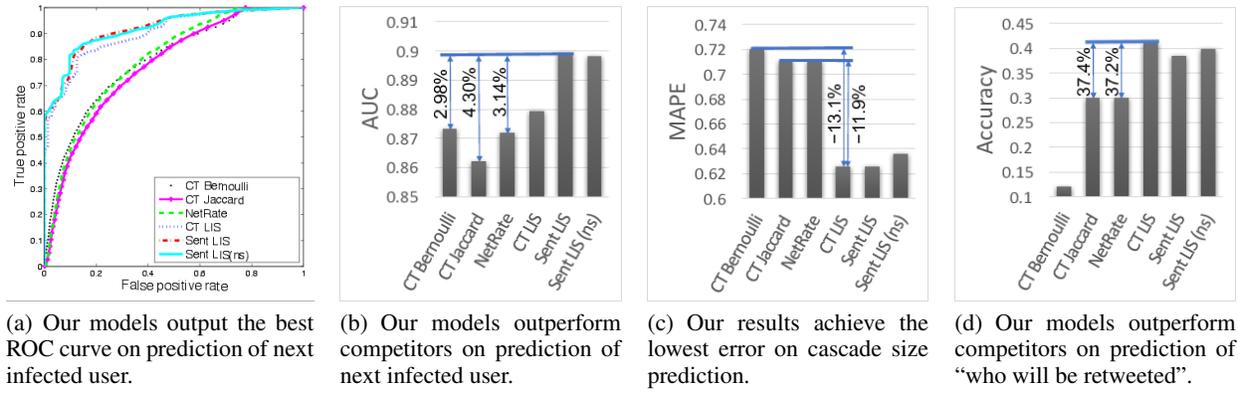


Figure 2: Our models are CT LIS, and its variants: Sent LIS and Sent LIS(ns). (a) The ROC curves of prediction results of next infected user. (b) The area under ROC curve (AUC) is used for next infected user prediction. (c) Mean absolute percentage error (MAPE) is used for cascade size prediction, and a good model should have small MAPE. (d) The top-one accuracy is used to measure the prediction accuracy of “who will be retweeted”.

Therefore we propose to define model parameters for individual users as opposed to user pairs, specifically users’ *influence vectors* and *susceptibility vectors*. For clarity, we use *interpersonal influence* to indicate the likelihood that information will be passed between two people, and *influence vector* to indicate a unilateral influence from a user and *susceptibility vector* is a unilateral susceptibility of a user. The interpersonal influences are modeled by the product of the influence vector from one user and the susceptibility vector from another. The advantages of our model named “CT LIS” is:

- **Dependency awareness:** our model captures the dependency of two interpersonal influences that are sending from the same user, or received by the same user, by the shared influence or the shared susceptibility vector respectively. For example, the interpersonal influence from c to d in Figure 1 is estimated with c ’s influence vector and d ’s susceptibility vector. The interpersonal influence of user c to user e contains c ’s influence vector as well. So, on account of the shared influence vector, the above two interpersonal influences couple with each other as expected. And interpersonal influence between user c and user d can be learned without overfitting.
- **Conciseness:** our model uses fewer parameters $O(n \cdot D)$, instead of $O(n^2)$ parameters for user pairs to represent users’ influence, where n is the number of users, and D is the dimension of influence and susceptibility vectors. Using a less complex model offers an advantage in modeling sparse data.
- **Effectiveness:** our model achieved the best performance on real Microblog data for three prediction tasks on: next infected user, cascade size, and “who will be retweeted” (see Figure 2).
- **Unification of temporal and categorical information:** our model proposes a unified framework based on temporal model, to make use of infection time, and categorical attributes, like sentiments and topics of review text.

2 Related Work

Previous work on cascade dynamics was studied based on point-process or influence models. [Zhao *et al.*, 2015; Shen *et al.*, 2014] used the variants of Poisson process to predict cascade size. Hawkes process was also studied to model the dynamics [Mavroforakis *et al.*, 2015; Wang *et al.*, 2016b]. [Du *et al.*, 2016a] proposed to use Recurrent Neural Network to predict the next point and time. The point-process based work model cascade dynamics in a macroscopic view, and did not explicitly consider the interpersonal influence.

In terms of influence models, scholars estimated interpersonal influences and their relationship to information propagation. Some of them made efforts to extract features that are related to propagation probability and learned from the observed information cascades [Crane and Sornette, 2008; Aral and Walker, 2012]. [Artzi *et al.*, 2012] predicted whether a user would respond to or retweet a message, thus being influenced, based on classification of demographic and content features. [Saito *et al.*, 2008] learned the propagation probability between neighbors of a directed network, using the orders of users become infected. [Goyal *et al.*, 2010] proposed to estimate the interpersonal influences, using assumptions from the Bernoulli model and Jaccard Index separately. NetInf [Gomez-Rodriguez *et al.*, 2010] modeled propagation probability, using exponential and power-law incubation time separately to infer the underlying network. [Tang *et al.*, 2009; Liu *et al.*, 2010] proposed a topic factor graph (TFG) to model the generative process of the topic-level social influence on large networks and heterogeneous networks respectively. LIS model [Wang *et al.*, 2015] learned users’ representations from the sequence of infected users, without temporal information.

Moreover, a series of work learned interpersonal influence with survival model and its variants to infer underlying networks. NetRate [Gomez-Rodriguez *et al.*, 2011] used survival theory to model the transmission rate between every user pair, which was viewed as an edge weight of the

influence network. [Gomez-Rodriguez *et al.*, 2013a] then modeled the hazard rate in a survival model with additive and multiplicative risks separately to improve the performance of cascade size prediction. Afterwards, InfoPath [Gomez-Rodriguez *et al.*, 2013b] was proposed to learn time-varying transmission rates for user pairs as the edge weights of the hidden dynamic network. The distribution of content topics has also been considered [Du *et al.*, 2013]. Taken together, these methods work in a pair-wise manner, *i.e.*, they learned the propagation probability between pairs of users. This approach is fundamentally different from the proposed method proposed in this paper, which focuses on inferring user-specific influence and susceptibility from historical cascades. Also influence representations on sentimental polarities can be learned in our model.

3 Learning Users' Influences

A temporal cascade C for actions on a target is defined as $C = \{(v_1, t_1), (v_2, t_2), \dots, (v_N, t_N) | t_1 \leq t_2 \leq \dots \leq t_N\}$, where v_i is the user who takes the action at time t_i , and N is the total number of acting users, *i.e.*, the cascade size. A temporal cascade is associated with an object, *e.g.*, a message, a product, or a hotel. To simplify the description of our model, we do not specify the identity of the target or message until we establish the overall objective function at the end.

To make our model more general, we assume that any pair of users can have an interpersonal influence, or probability of passing information between them. A very small or zero value of influence can capture the underlying disconnections of the user network, and vice versa. When a social network is available, we can easily apply it in our model as a constraint that only connected users can influence each other.

3.1 Survival Analysis Model

Before presenting our model, we introduce the prior knowledge of the Survival Analysis Model [Lawless, 2011], which is used to model life time of a species exploring to some hazard environment. We mimic the life time as the incubation time before a user being infected and taking an action. Thus we define the infection time T of a user as a continuous random variable, with $T \in [0, \infty)$. Let $f(t)$ and $F(t)$ denote the probability density function (PDF) and the cumulative density function (CDF) respectively. The probability $Pr(T \leq t) = F(t)$. So the probability of a user not taking the action until time t is defined by the survivor function

$$S(t) = Pr(T \geq t) = 1 - F(t) = \int_t^\infty f(x)dx.$$

Given that users survive until time t , a hazard function $h(t)$ for users is defined as the instantaneous infection rate in time interval $[t, t + \varepsilon)$ in a hazard situation, where ε is an infinitesimal elapsed time:

$$h(t) = \lim_{\varepsilon \rightarrow 0} \frac{Pr(t \leq T < t + \varepsilon | T \geq t)}{\varepsilon} = \frac{f(t)}{S(t)}.$$

Noticing that $f(t) = -S'(t)$ and $S(0) = 1$, the survivor function can be expressed as

$$\ln S(x) = - \int_0^x h(x)dx. \tag{1}$$

3.2 Our Proposed Model

Our model represents a user v_i with two non-negative D -dimensional vectors I_i and S_i , which stand for influence representation and susceptibility representation respectively. D is a parameter for the size of vectors which is given. Without loss of generality, we can turn the representations into matrices to consider sentimental polarities. Each row of the matrices is the representation vector on a sentimental polarity. Influence matrix \mathbf{I}_i and susceptibility matrix \mathbf{S}_i have $K \times D$ dimensions, where K is the number of sentimental polarities or classes. The sentiment of information is defined as a one-of- K vector o . Only one element in vector o can be 1 with the others being zero, indicating that the information belongs to that corresponding sentiment class. When $K = 1$ and $o = 1$, the model reverts back to vector representations of no sentiments. Thus we introduce our model in a general form with sentiment o in the following sections.

For a cascade with sentiment o , the transmission rate function $\phi(\cdot)$ from users v_j to v_i , is defined by equation:

$$\phi(\mathbf{I}_j, \mathbf{S}_i, o) = 1 - \exp\{-o^T \mathbf{I}_j \mathbf{S}_i^T o\} \tag{2}$$

where matrix \mathbf{I}_j and matrix \mathbf{S}_i are parameters that capture the influence of user v_j and the susceptibility of user v_i respectively. The transmission rate function (2) indicates the likelihood of successful passing of information between them. We use an exponential function to scale the transmission rate between 0 and 1 for regularization. So the extent of an interpersonal influence is calculated by equation (2).

To simplify, let \mathcal{H}_{ji} denote the set of parameters $\{\mathbf{I}_j, \mathbf{S}_i, o\}$. With a transmission rate $\phi(\mathcal{H}_{ji})$, we define the hazard function of the Survival Analysis Model for user v_i at time t , under the influence from v_j , as follows:

$$h(t|t_j; \phi(\mathcal{H}_{ji})) = \phi(\mathbf{I}_j, \mathbf{S}_i, o) \frac{1}{t - t_j + 1}, \tag{3}$$

where $t - t_j + 1$ depicts the hazard function monotonously decaying with the time elapsed from t_j . Adding 1 avoids an unbounded hazard rate due to a zero or infinitesimal value of $t - t_j$. Since equation (3) holds only when $t \geq t_j$, we define the hazard rate $h(t|t_j; \phi(\mathcal{H}_{ji})) = 0$, when $t < t_j$, namely, user v_j has not been infected at time t . Moreover, as mentioned earlier, we can consider social network as another constraint by defining hazard function $h(t|t_j; \phi(\mathcal{H}_{ji})) = 0$, if user v_i and user v_j are not connected.

Given the survivor function (1) in the Survival Analysis Model, the survivor function $S(t|t_j; \phi(\mathcal{H}_{ji}))$ that user v_i survives longer than t satisfies

$$\begin{aligned} \ln S(t|t_j; \phi(\mathcal{H}_{ji})) &= - \int_0^t h(x|t_j; \phi(\mathcal{H}_{ji}))dx \\ &= \phi(\mathbf{I}_j, \mathbf{S}_i, o) \cdot \ln(t - t_j + 1) \end{aligned} \tag{4}$$

Finally, given that influential user v_j takes action or becomes infected at time t_j , the probability density function of user v_i happening (acting on the target) at time t is

$$f(t|t_j; \phi(\mathcal{H}_{ji})) = h(t|t_j; \phi(\mathcal{H}_{ji}))S(t|t_j; \phi(\mathcal{H}_{ji})).$$

With the assumption that a user is only infected by one of the previously infected users, the likelihood of user $v_i, i > 1$

being infected at time t_i in a cascade is

$$\begin{aligned} f(t_i|\mathbf{t}; \phi(\mathcal{H})) &= \sum_{j:t_j < t_i} f(t_i|t_j; \phi(\mathcal{H}_{ji})) \prod_{k \neq j, t_k < t_i} S(t_i|t_k; \phi(\mathcal{H}_{ki})) \\ &= \sum_{j:t_j < t_i} h(t_i|t_j; \phi(\mathcal{H}_{ji})) \cdot \prod_{k:t_k < t_i} S(t_i|t_k; \phi(\mathcal{H}_{ki})). \end{aligned}$$

Thus given that user v_1 takes the first action at time t_1 , the joint likelihood of observing the whole cascade is

$$f(\mathbf{t} \setminus t_1|t_1; \phi(\mathcal{H})) = \prod_{i>1} \sum_{j:t_j < t_i} h(t_i|t_j; \phi(\mathcal{H}_{ji})) \cdot \prod_{k:t_k < t_i} S(t_i|t_k; \phi(\mathcal{H}_{ki})).$$

To consider the negative cases, we define a time window of our observation for cascade C . The end of the time window is t_E , and $t_E > t_N$. The users who do not act until t_E are survivors under the influence of infected users. Thus the probability of a negative case for the survival of user v_l is

$$S(t_E|\mathbf{t}; \phi(\mathcal{H})) = \prod_{i:t_i \leq t_N} S(t_E|t_i; \phi(\mathcal{H}_{il})).$$

Considering the negative cases, the log-likelihood of a cascade is

$$\begin{aligned} \ln \mathcal{L}(\mathbf{I}, \mathbf{S}; o) &= \sum_{i>1} \ln \left(\sum_{j:t_j < t_i} \phi(\mathbf{I}_j, \mathbf{S}_i, o) \frac{1}{t_i - t_j + 1} \right) - \\ &\quad \sum_{i>1} \sum_{k:t_k < t_i} \phi(\mathbf{I}_k, \mathbf{S}_i, o) \cdot \ln(t_i - t_k + 1) - \\ &\quad \sum_{l=1}^L \mathbb{E}_{v_l \sim P(u)} \left[\sum_{j=1}^N \phi(\mathbf{I}_j, \mathbf{S}_l, o) \cdot \ln(t_E - t_j + 1) \right] \end{aligned}$$

The negative cases contain any pair of an infected user and a surviving user. The number of survivors is always the majority of the overall social network. Thus the number of negative user pairs is much larger than that of positive pairs in a cascade. For learning efficiency, we adopt the negative sampling strategy [Mikolov *et al.*, 2013]. We sample L users as negative cases according to the distribution $P(u) \propto R_u^{3/4}$, where R_u is the frequency of user u becoming infected in a cascade. It is worth noticing that sampling of negative cases is repeated in every optimization iteration to honor the expectation. The infection frequency of a user indicates how easily he or she could become infected again. Observing a frequently infected user who survives provides more information regarding the likelihood. Sampling negative cases from the distribution of users' infected frequencies is a better choice.

Finally, the optimization problem of learning users' influence representations and susceptibility representations is

$$\min_{\mathbf{I}, \mathbf{S}} - \sum_C \ln \mathcal{L}^c(\mathbf{I}, \mathbf{S}; o^c) \quad (5a)$$

$$s.t. \quad \mathbf{I}_{ki} \geq \mathbf{0}, \mathbf{S}_{ki} \geq \mathbf{0}, \forall k, i. \quad (5b)$$

where superscript c is used to identify the values or functions that are related to cascade C . The log-likelihood of all the observed cascades is summarized in the above objective function.

3.3 Optimization

The model learns the distributed representations of users' influences, by means of a gradient algorithm. The gradients of the transmission rate function on matrix \mathbf{I}_v and matrix \mathbf{S}_u are

$$\begin{aligned} \frac{\partial \phi(\mathbf{I}_v, \mathbf{S}_u, o)}{\partial \mathbf{I}_v} &= (1 - \phi(\mathbf{I}_v, \mathbf{S}_u, o)) o o^T \mathbf{S}_u \\ \frac{\partial \phi(\mathbf{I}_v, \mathbf{S}_u, o)}{\partial \mathbf{S}_u} &= (1 - \phi(\mathbf{I}_v, \mathbf{S}_u, o)) o o^T \mathbf{I}_v \end{aligned}$$

The gradients are $K \times D$ matrices. Only the k -th row in each matrix has a non-zero gradient, when a cascade belongs to the k -th sentiment class, *i.e.*, $o_k = 1$.

As the negative cases for a cascade are repeatedly sampled in every iteration, we define $[\mathbb{V}_s^c]_\tau$ as the set of negative users in the τ -th iteration of the algorithm for cascade C :

$$[\mathbb{V}_s^c]_\tau = \{v_l \sim P(u)\}_L,$$

where L is the set size. Moreover, Only when user v becomes infected in a cascade, *i.e.*, $t_1 \leq t_v \leq t_N$, the gradients of the log-likelihood (5a) on matrix \mathbf{I}_v are non-zero; Only when user v is infected and $t_1 < t_v \leq t_N$, or user v is in a negative case, the gradients on matrix \mathbf{S}_v are non-zero; otherwise, the gradients are always zeros.

Therefore, the gradients of the objective function (5a) on matrix \mathbf{I}_v and matrix \mathbf{S}_v are

$$\begin{aligned} g_{I_v} &= - \sum_c \mathbf{1}(t_v^c \leq t_N^c) \frac{\partial \mathcal{L}^c(\mathbf{I}, \mathbf{S}; o^c)}{\partial \mathbf{I}_v} \\ g_{S_v} &= - \sum_c \mathbf{1}(t_1^c < t_v^c \leq t_N^c) \frac{\partial \mathcal{L}^c(\mathbf{I}, \mathbf{S}; o^c)}{\partial \mathbf{S}_v} + \\ &\quad \sum_c \mathbf{1}(v \in [\mathbb{V}_s^c]_\tau) \cdot \sum_{j=1}^{N^c} (1 - \phi(\mathbf{I}_j, \mathbf{S}_v, o^c)) \cdot \ln(t_E^c - t_j^c + 1) o^c o^{cT} \mathbf{I}_j \end{aligned}$$

where $\mathbf{1}(\cdot)$ is an indicator function, with an output of 1 if the argument is true, and 0 otherwise. The gradients g_{I_v} and g_{S_v} are $K \times D$ matrices.

The framework of Stochastic Gradient Descent (SGD) over shuffled mini-batches was employed for efficient optimization. The mini-batch size was set at 12 cascades. To solve the non-negative constraints on parameters, Projected Gradient (PG) was used to adjust the gradients. Moreover, since deciding the learning rate is not trivial, we chose Adadelta to adaptively tune the learning rate with an insensitive decay constant $\rho = 0.95$ as suggested in [Zeiler, 2012].

4 Experiments

To evaluate our model, we used real Microblog data crawled from Sina Weibo¹ in which users' activity in passing messages is publicly available. The temporal cascades were extracted for all the messages in the data for evaluations.

¹Sina Weibo (<http://www.weibo.com>), is one of the biggest Microblog websites in China.

4.1 Data and Setup

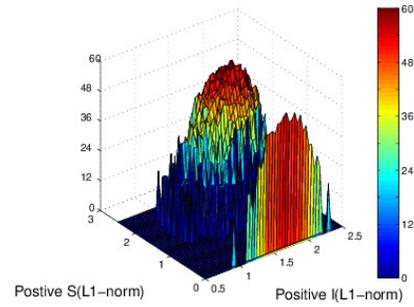
We have an initial pool of 315.6 million records including posting, retweet, and mentioning of messages between Nov 1, 2013 and Feb 28, 2014 from the timelines of 312,000 users, from the Sina Weibo database. We filtered and chose the messages with frequently used emoticons. Emoticons are labeled with positive or negative sentiment; e.g., :) and :D express positive emotion, whereas :(and :-(express negative emotion, in order to determine the message’s sentiment label. In fact, any reliable sentiment classifier can also be used to determine the sentiments, which is out of our reach. In our experiments, we choose emoticons to label message sentiments without loss of generality, and we have $K = 2$ sentiments. Since some parts of cascades might be missing, we crawled the missing retweet records for those chosen cascades that are not integrate in the data pool. Cascades of sizes less than 8 were removed to ensure that the messages examined have attracted enough attention. The resulting sample contained 6,219 active users, and a total of 44,021 cascades from Oct 31, 2013 to Mar 3, 2014. The preprocessed data start earlier than the original data because we withdrew the missing data from the messages.

To set up the experiments, the cascades were evenly split into 10 groups. Ten-fold cross-testing is used for our evaluations, alternately training 9 of 10 groups and testing the remaining one. As we discussed in the previous work, the most representative influence models that used the same information as our model are used as competitors: NetRate, continuous version of Jaccard and Bernoulli models (denoted as CT Jaccard and CT Bernoulli). Our CT LIS model has another two variants: Sent LIS with sentiment information, Sent LIS (ns) with negative sampling. With testing on vector size of users’ representations, we choose $D = 8$ for both efficiency and stable objective value.

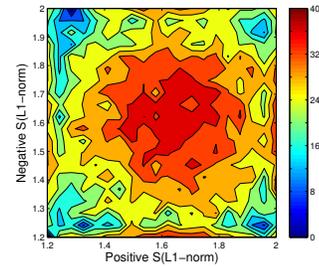
4.2 Study of Users’ Influences and Susceptibilities

We present the distributions of influential and susceptible users from our results. With positive and negative sentiments, a user can have four vectors (from the two matrices): Positive I, Negative I, Positive S, and Negative S. We study those row vectors with L1-norms, i.e., the summation of the absolute value of each element. Thus we can use those L1-norms as coordinates of a point for each user. Figure 3 shows the contour maps to visualize the user distributions in different influence and susceptibility coordinate systems.

The distribution of “Positive S vs. Positive I” in Figure 3 (a) interestingly shows two groups of users in positive sentiment class, corresponding to two peaks in the figure. The group along the bottom axis has very lower susceptibilities but significant influences. The upper right group has both significant influences and susceptibilities. We will refer to these two groups of people as *primary influential* and *secondary influential*, respectively. The primary influential people have the power to influence other users, without being infected easily, as was also explained by Aral and Walker on Facebook users [Aral and Walker, 2012]. Interestingly, on Sina Weibo, users can get influence credit, or have more people retweet them, by being an agency or hub. So people invest considerable effort in retweeting (potentially) interesting messages



(a) Positive S vs. Positive I



(b) Negative S vs. Positive S

Figure 3: Analysis of L1-norm of latent representations on sentimental polarities.

to attract others to follow them and retweet from them. This type of user is not restricted to the Sina Weibo scenario. Some primary influential people like to explore new restaurants and make recommendations to their friends or audiences. Another type of user simply likes to browse other people’s recommendations or ratings and advertise them to their own audiences. Similar activities might be seen in place of interest (POI) recommendation, hotel bookings, and online shopping as well. As for an online system, both primary influential and secondary influential people are important. The primary influential users represent the originating power of the system to bring new resources and initiate a cold start. The secondary influential users are good advertisers or hubs to enable other people to get information efficiently. As the primary influential people are considered high-quality users by system operators, the secondary influential ones may easily be persuaded to help in sharing advertisements. And on the negative sentiment class, we can also find the two groups of users.

In addition, from the user distribution on susceptibility vectors in Figure 3 (b), we can see that although a large group of users has the same significant susceptibilities (a large hot area in the middle), many users may be more susceptible to different sentimental messages, as shown in some hot areas closed to the four edges of the figure. We can also observe the similar distribution on influence vectors.

4.3 Prediction of Next Infected User

This task aims at predicting whether a user v will take an action (i.e., become infected) given time t . For every user, we calculate the likelihood of becoming infected. Thus we can

use AUC of the ROC (receiver operating characteristic) curve (see Figure 2(a)), to measure the output likelihood.

The ROC curves in Figure 2(a) show that our models achieve better performance than list-wise models, considering the areas under the curves. All our variants, achieve higher AUC values in the classification metric.

In Figure 2(b), the average results of 10-fold cross-tests are reported. The figure shows that our CT LIS achieved consistent better AUC than the three baselines. And with sentiment information, our Sent LIS improved the AUC accuracy by at most 4.30%. Moreover, considering sentiment information improved the performance on this prediction task. Although Sent LIS(ns) cannot outperform Sent LIS, but the former’s training is more efficient, since of the random sampled negative cases.

4.4 Cascade Size Prediction

Cascade size prediction (popularity) is a key part of influence maximization and viral marketing applications. In the application, we chose the first P user-time pairs in each cascade as the initial status, and we predicted the cascade size at time t_N , $t_N > t_P$. t_P is the infecting time of the last user in the initial tuples. We made our prediction by simulating the generation process of a cascade.

The time interval $t_N - t_P$ is first evenly divided into discrete time points. Starting from the time point right after t_P , every infected user u makes a random trial to infect user v at each time point $\tau_i > t_P$. The probability in a trial is

$$Pr(T \leq \tau_i | t_u; \phi(\mathcal{H}_{u,v})) = \frac{\int_{\tau_{i-1}}^{\tau_i} f(t | t_u; \phi(\mathcal{H}_{u,v})) dt}{S(\tau_{i-1} | t_u; \phi(\mathcal{H}_{u,v}))}.$$

This is a conditional probability, given that user v will survive until time τ_{i-1} . Users who become infected in a random trial are added to the number of infected users for the next step of the simulation process. Thus, we use the *mean absolute percentage error* (MAPE) to measure the predictions with ground truth cascade sizes, where a smaller value indicates a better prediction. In the experiments, we chose first $P = 10$ users in a cascade as the initialization for the prediction. The simulations were repeated 100 times for every cascade in the test data, and the results were averaged to arrive at the prediction result.

Figure 2(c) shows that the best prediction result come from our models, achieving at least 11.9% MAPE reduction compared to the pair-wise models. Besides, considering sentiment or not did not bring much differences in our cascade size prediction, while the small differences may be the result of noisy sentiment labels.

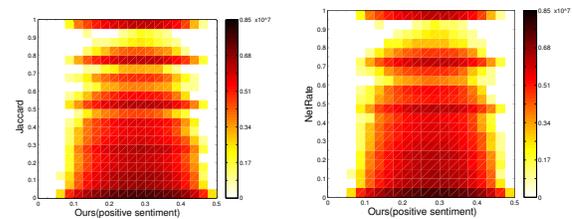
4.5 Prediction of Who Will Be Retweeted

“Who will be retweeted” (WBR) is a new application that helps to identify the causality of who influences whom to take an action. For example, it enables us to find out who has influenced or motivated the target user to retweet a message, “like” a webpage, buy a product, or go to some location. The relations of who retweets whom are extracted as previously described, which is treated as the ground truth. We use average *Accuracy* (Acc) of top-one prediction as metric.

Our results in causality judgment of who influences whom achieve more than 37.2% in the accuracy metric, as Figure 2(d) shows. Therefore, our models outperformed the pair-wise models, without suffering from the over-fitting problem in causality judgment.

4.6 Discrimination of Interpersonal Influences

Figure 4 shows the heat map distribution of users’ interpersonal influence values. In the two sub-figures, very hot and dark cells horizontally line at the bottom, with a range from 0.1 to 0.4. For the influences of those user pairs, our model discriminates the influential degrees from 0.1 to 0.4. In addition, our model shows a discriminating distribution of interpersonal influences at the higher values of the evaluation models. In summary, the figure suggests that our values are more discriminating, which can guarantee a better application performance.



(a) Our interpersonal influence vs. CT Jaccard’s (b) Ours interpersonal influence vs. NetRate’s

Figure 4: Heat map of interpersonal influences. Ours is more discriminating

5 Conclusions

In this study, we have proposed a model to learn the concise representations of users’ influence from their historical behaviors. The contributions of our model include:

- **Dependency awareness:** our model captures the dependency of two interpersonal influences that are sending from the same user, or received by the same user, by the shared influence or the shared susceptibility vector respectively.
- **Conciseness:** our model use fewer parameters, offering an advantage in modeling sparse data.
- **Effectiveness:** Our model achieved the best performance on real Microblog data for three prediction tasks.
- **Unification of temporal and categorical information:** our model applies a unified framework based on temporal model, which can make use of sentiment information easily.

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