

Information Bottleneck Approach to Spatial Attention Learning

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Abstract

The selective visual attention mechanism in the human visual system (HVS) restricts the amount of information to reach visual awareness for perceiving natural scenes, allowing near real-time information processing with limited computational capacity [Koch and Ullman, 1987]. This kind of selectivity acts as an ‘Information Bottleneck (IB)’, which seeks a trade-off between information compression and predictive accuracy. However, such information constraints are rarely explored in the attention mechanism for deep neural networks (DNNs). In this paper, we propose an IB-inspired spatial attention module for DNN structures built for visual recognition. The module takes as input an intermediate representation of the input image, and outputs a variational 2D attention map that minimizes the mutual information (MI) between the attention-modulated representation and the input, while maximizing the MI between the attention-modulated representation and the task label. To further restrict the information bypassed by the attention map, we quantize the continuous attention scores to a set of learnable anchor values during training. Extensive experiments show that the proposed IB-inspired spatial attention mechanism can yield attention maps that neatly highlight the regions of interest while suppressing backgrounds, and bootstrap standard DNN structures for visual recognition tasks (*e.g.*, image classification, fine-grained recognition, cross-domain classification). The attention maps are interpretable for the decision making of the DNNs as verified in the experiments. Our code is available at this [https](https://github.com/qiuxialai/ib-spatial-attention) URL.

1 Introduction

Human beings can process vast amounts of visual information in parallel through visual system [Koch *et al.*, 2006] because the attention mechanism can selectively attend to the most informative parts of visual stimuli rather than the whole scene [Eriksen and Hoffman, 1972]. A recent trend is to incorporate attention mechanisms into deep neural networks

(DNNs), to focus on task-relevant parts of the input automatically. Attention mechanism has benefited sequence modeling tasks as well as a wide range of computer vision tasks to boost the performance and improve the interpretability.

The attention modules in CNNs can be broadly categorized into *channel-wise attention* and *spatial attention*, which learns channel-wise [Hu *et al.*, 2018] and spatially-aware attention scores [Simonyan *et al.*, 2013] for modulating the feature maps, respectively. As channel-wise attention would inevitably lose spatial information essential for localizing the important parts, in this paper, we focus on the spatial attention mechanism. There are *query-based* and *module-based* spatial attention learning methods. Query-based attention, or ‘self-attention’, generates the attention scores based on the similarity/compatibility between the query and the key content. Though having facilitated various computer vision tasks, such dense relation measurements would lead to heavy computational overheads [Han *et al.*, 2020], which significantly hinders its application scenario. Module-based attention directly outputs an attention map using a learnable network module that takes as input an image/feature. Such an end-to-end inference structure is more efficient than query-based attention, and has been shown to be effective for various computer vision tasks. Existing spatial attention mechanisms trained for certain tasks typically generate the attention maps by considering the contextual relations of the inputs. Although the attention maps are beneficial to the tasks, the attention learning process fails to consider the inherent information constraints of the attention mechanism in HVS, *i.e.*, to ensure that the information bypassed by the attention maps is of minimal redundancy, and meanwhile being sufficient for the task.

To explicitly incorporate the information constraints of the attention mechanism in HVS into attention learning in DNNs, in this paper, we propose an end-to-end trainable spatial attention mechanism inspired by the ‘Information Bottleneck (IB)’ theory. The whole framework is derived from an information-theoretic argument based on the IB principle. The resulted variational attention maps can effectively filter out task-irrelevant information, which reduces the overload of information processing while maintaining the performance. To further restrict the information bypassed by the attention map, an adaptive quantization module is incorporated to round the attention scores to the nearest anchor value. In this way, previous continuous attention values are replaced

by a finite number of anchor values, which further compress the information filtered by the attention maps. To quantitatively compare the interpretability of the proposed attention mechanism with others, we start from the definition of interpretability on model decision making, and measure the interpretability in a general statistical sense based on the attention consistency between the original and the modified samples that do not alter model decisions.

In summary, our contributions are three-fold:

- We propose an IB-inspired spatial attention mechanism for visual recognition, which yields variational attention maps that minimize the MI between the attention-modulated representation and the input while maximizing the MI between the attention-modulated representation and the task label.
- To further filter out irrelevant information, we design a quantization module to round the continuous attention scores to several learnable anchor values during training.
- The proposed attention mechanism is shown to be more interpretable for the decision making of the DNNs compared with other spatial attention models.

Extensive experiments validate the theoretical intuitions behind the proposed IB-inspired spatial attention mechanism, and show improved performances and interpretability for visual recognition tasks.

2 Related Work

2.1 Spatial Attention Mechanism in DNNs

Attention mechanisms enjoy great success in sequence modeling tasks such as machine translation [Bahdanau *et al.*, 2015], speech recognition [Chorowski *et al.*, 2015] and image captioning [Xu *et al.*, 2015]. Recently, they are also shown to be beneficial to a wide range of computer vision tasks to boost the performance and improve the interpretability of general CNNs. The attention modules in CNNs fall into two broad categories, namely channel-wise attention and spatial attention. The former learns channel-wise attention scores to modulate the feature maps by reweighing the channels [Hu *et al.*, 2018]. The latter learns a spatial probabilistic map over the input to enhance/suppress each 2D location according to its relative importance *w.r.t.* the target task [Simonyan *et al.*, 2013]. In this section, we focus on spatial attention modules.

Query-based/ Self-attention. Originated from query-based tasks [Bahdanau *et al.*, 2015; Xu *et al.*, 2015], this kind of attention is generated by measuring the similarity/compatibility between the query and the key content. Seo *et al.* [2018] use a one-hot encoding of the label to query the image and generate progressive attention for attribute prediction. Jetley *et al.* [2018] utilize the learned global representation of the input image as a query and calculate the compatibility with local representation from each 2D spatial location. Hu *et al.* [2019] adaptively determines the aggregation weights by considering the compositional relationship of visual elements in local areas. Query-based attention considers dense relations in the space, which can improve the discriminative ability of CNNs. However, the non-negligible computational overhead limits

its usage to low-dimensional inputs, and typically requires to downsample the original images significantly.

Module-based attention. The spatial attention map can also be directly learned using a softmax-/sigmoid-based network module that takes an image/feature as input and outputs an attention map. Being effective and efficient, this kind of attention module has been widely used in computer vision tasks such as action recognition [Sharma *et al.*, 2015] and image classification [Woo *et al.*, 2018]. Our proposed spatial attention module belongs to this line of research, and we focus on improving the performance of visual recognition over baselines without attention mechanisms.

Previous spatial attention learning works focus on the relations among non-local or local contexts to measure the relative importance of each location, and do not consider the information in the feature filtered by the attention maps. We instead take inspiration from the IB theory [Tishby *et al.*, 1999] which maintains a good trade-off between information compression and prediction accuracy, and propose to learn spatial attention that minimizes the MI between the masked feature and the input, while maximizing the MI between the masked feature and the task label. Such information constraints could also help remove the redundant information from the input features compared with conventional relative importance learning mechanisms.

2.2 IB-Inspired Mask Generation

IB theory has been explored in tasks such as representation learning [Alemi *et al.*, 2017; Achille and Soatto, 2018] and domain adaptation [Du *et al.*, 2020]. Here, we focus on IB-inspired mask generation methods, which yield additive [Schulz *et al.*, 2019] or multiplicative masks [Achille and Soatto, 2018; Taghanaki *et al.*, 2019; Zhmoginov *et al.*, 2019] to restrict the information that flows to the successive layers.

Information Dropout [Achille and Soatto, 2018] multiplies the layer feature with a learnable noise mask to control the flow of information. This is equivalent to optimizing a modified cost function that approximates the IB Lagrangian of [Tishby *et al.*, 1999], allowing the learning of a sufficient, minimal and invariant representation for classification tasks. InfoMask [Taghanaki *et al.*, 2019] filters out irrelevant background signals using the masks optimized on IB theory, which improves the accuracy of localizing chest disease. Zhmoginov *et al.* [2019] generates IB-inspired Boolean attention masks for image classification models to completely prevent the masked-out pixels from propagating any information to the model output. Schulz *et al.* [2019] adopts the IB concept for interpreting the decision-making of a pre-trained neural network, by adding noise to intermediate activation maps to restrict and quantify the flow of information. The intensity of the noise is optimized to minimize the information flow while maximizing the classification score.

In this paper, we propose an IB-inspired spatial attention mechanism based on a new variational approximation of the IB principle derived from a neural network incorporated with attention module ($\mathcal{L}_{\text{AttVIB}}$ in Eq. (6)). Compared with the above works, our optimization objective is not derived from the original IB Lagrangian of [Tishby *et al.*, 1999], thus the resulted attention mechanism is parameterized with different

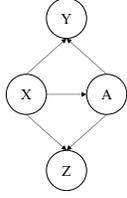


Figure 1: **Graphical model** of the probabilistic neural network with IB-inspired spatial attention mechanism (§3.2).

network architectures. Besides, we focus on learning continuous spatial attention instead of noise masks [Achille and Soatto, 2018; Schulz *et al.*, 2019], which is also different from the Boolean attention in [Zhmoginov *et al.*, 2019].

3 Methodology

3.1 Overview

We derived the framework of the proposed spatial attention mechanism theoretically from the IB principle on a neural network incorporated with an attention module. Assuming that random variables X, Y, A and Z follow the joint conditional distribution of the model shown in Fig. 1. Here, X, Y, A and Z denote the input, output, spatial attention map, and the latent representation obtained from X and A , respectively. We drive the proposed spatial attention framework based on the joint distribution and the IB principle. The resulted framework is shown in Fig. 2, which consists of an attention module $p(a|x)$, a set of anchor values $\{v_i\}$ for quantization, an encoder $p(z|x, a)$, and a decoder $q(y|z)$.

The input x is first passed through the attention module $p(a|x)$ to produce a continuous variational attention map a , which is quantized to a discrete attention map a_q using a set of learnable anchor values v_i . Then, a_q and x are encoded to a latent vector z , and decoded to a prediction y . The whole framework is trained end-to-end using the loss function defined in Eq. (10). The derivation of the framework is shown in §3.2, and more details are provided in the supplementary. The attention score quantization process is shown in §3.3.

3.2 IB-inspired Spatial Attention Mechanism

We introduce the IB principle [Tishby *et al.*, 1999] to learn the spatial attention that minimizes the MI between the masked representation and the input, while maximizing the MI between the masked representation and the class label. Different from [Alemi *et al.*, 2017] for a standard learning framework, we derive new variational bounds of MI within an *attentive framework* for visual recognition, which lead to an IB-inspired spatial attention mechanism.

Let the random variables X, Y, A and Z denote the input, output, spatial attention map, and the latent representation obtained from X and A , respectively. The MI between the latent feature Z and its output Y is defined as:

$$I(Z; Y) = \int p(y, z) \log \frac{p(y|z)}{p(y)} dy dz. \quad (1)$$

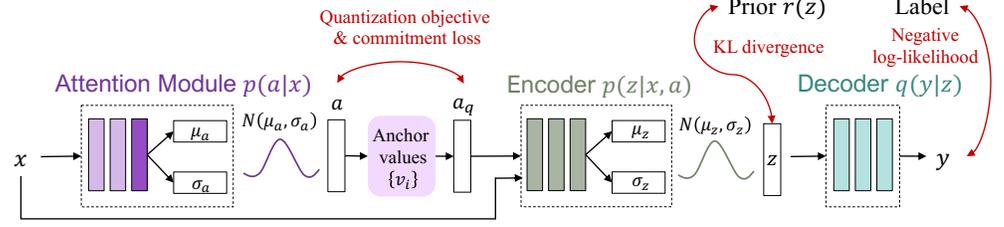


Figure 2: **Framework of the IB-inspired spatial attention mechanism for visual recognition.** The input x is passed through an attention module to produce a continuous variational attention map a , which is quantized to a discrete attention map a_q using a set of learnable anchor values v_i . Then, a_q and x are encoded to a latent vector z , and decoded to a prediction y . Loss function in Eq. (10). See §3.2 and §3.3.

We introduce $q(y|z)$ to be a variational approximation of the intractable $p(y|z)$. Since the Kullback Leibler (KL) divergence is always non-negative, we have:

$$\begin{aligned} D_{\text{KL}}[p(y|z)||q(y|z)] &= \int p(y|z) \log \frac{p(y|z)}{q(y|z)} dy \geq 0 \\ \Rightarrow \int p(y|z) \log p(y|z) dy &\geq \int p(y|z) \log q(y|z) dy, \end{aligned} \quad (2)$$

which leads to

$$I(Z; Y) \geq \int p(y, z) \log q(y|z) dy dz + H(Y), \quad (3)$$

where $H(Y) = -\int p(y) \log p(y) dy$ is the entropy of Y , which is independent of the optimization procedure thus can be ignored. By leveraging the fact that $p(y, z) = \int p(x, y, z, a) dx da = \int p(x) p(a|x) p(y|x, a) p(z|x, a) dx da$ (see Fig. 1), and ignoring $H(Y)$, the new variational lower bound is as follows:

$$I(Z; Y) \geq \int p(x, y) p(a|x) p(z|x, a) \log q(y|z) dx da dy dz, \quad (4)$$

where $p(a|x)$ is the attention module, $p(z|x, a)$ is the encoder, and $q(y|z)$ is the decoder. $I(Z; Y)$ can thus be maximized by maximizing its variational lower bound.

Next, to minimize the MI between the attention-modulated representation and the input, we consider $I(Z; X, A)$, and obtain the following upper bound:

$$I(Z; X, A) \leq \int p(x) p(a|x) p(z|x, a) \log \frac{p(z|x, a)}{r(z)} dx da dz, \quad (5)$$

where $r(z)$ is a prior distribution of z . In our experiments, we use a spherical Gaussian $\mathcal{N}(z|0, I)$ as the prior $r(z)$.

By combining Eq. (4) and (5), we obtain the lower bound of the attentive variational information bottleneck:

$$\begin{aligned} \mathcal{L}_{\text{AttVIB}} &\equiv I(Z; Y) - \beta I(Z; X, A) \\ &= \int p(x, y) p(a|x) p(z|x, a) \log q(y|z) dx da dy dz \\ &\quad - \beta \int p(x) p(a|x) p(z|x, a) \log \frac{p(z|x, a)}{r(z)} dx da dz, \end{aligned} \quad (6)$$

which offers an IB-inspired spatial attention mechanism for visual recognition. Here, $\beta > 0$ controls the tradeoff between information compression and prediction accuracy.

We approximate $p(x)$, $p(x, y)$ with empirical distribution $p(x) = \frac{1}{N} \sum_{n=1}^N \delta_{x_n}(x)$, $p(x, y) = \frac{1}{N} \sum_{n=1}^N \delta_{x_n}(x) \delta_{y_n}(y)$

following [Alemi *et al.*, 2017], where N is the number of training samples, x_n and (x_n, y_n) are samples drawn from data distribution $p(x)$ and $p(x, y)$, respectively. The approximated lower bound $\mathcal{L}_{\text{AttVIB}}$ can thus be written as:

$$\begin{aligned} \tilde{\mathcal{L}}_{\text{AttVIB}} = & \frac{1}{N} \sum_{n=1}^N \left\{ \int p(a|x_n) p(z|x_n, a) \log q(y_n|z) da dz \right. \\ & \left. - \beta \int p(a|x_n) p(z|x_n, a) \log \frac{p(z|x_n, a)}{r(z)} da dz \right\}. \end{aligned} \quad (7)$$

Similar to [Alemi *et al.*, 2017], we suppose to use the attention module of the form $p(a|x) = \mathcal{N}(a|g_e^\mu(x), g_e^\Sigma(x))$, and the encoder of the form $p(z|x, a) = \mathcal{N}(z|f_e^\mu(x, a), f_e^\Sigma(x, a))$, where g_e and f_e are network modules. To enable back-propagation, we use the reparametrization trick [Kingma and Welling, 2014], and write $p(a|x)da = p(\varepsilon)d\varepsilon$ and $p(z|x, a)dz = p(\epsilon)d\epsilon$, where $a = g(x, \varepsilon)$ and $z = f(x, a, \epsilon)$ are deterministic functions of x and the Gaussian random variables ε and ϵ . The loss function is:

$$\begin{aligned} \mathcal{L} = & -\frac{1}{N} \sum_{n=1}^N \{ \mathbb{E}_{\varepsilon \sim p(\varepsilon)} [\mathbb{E}_{\epsilon \sim p(\epsilon)} [\log q(y_n | f(x_n, g(x_n, \varepsilon), \epsilon))]] \\ & + \beta \mathbb{E}_{\varepsilon \sim p(\varepsilon)} [D_{\text{KL}} [p(z|x_n, g(x_n, \varepsilon)) \parallel r(z)]] \}. \end{aligned} \quad (8)$$

The first term of the loss function is the negative log-likelihood of the prediction, where the label y_n of x_n is predicted from the latent encoding z , and z is generated from x_n and its attention map $a = g(x_n, \varepsilon)$. Minimizing this term leads to maximal prediction accuracy. The second term is the KL divergence between distributions of latent encoding z and the prior $r(z)$, the minimization of which enables the model to learn an IB-inspired spatial attention mechanism for visual recognition. This is different from the regular IB principle [Tishby *et al.*, 1999; Alemi *et al.*, 2017] which is only for the representation learning without attention module.

3.3 Attention Score Quantization

We define the continuous attention space as $A \in \mathbb{R}^{W_a \times H_a}$, and the quantized attention space as $A_q \in \mathbb{R}^{W_a \times H_a}$, where W_a, H_a are the width and height of the attention map, respectively. As shown in Fig. 2, the input x is passed through an attention module to produce a continuous variational attention map a , which is mapped to a discrete attention map a_q through a nearest neighbour look-up among a set of learnable anchor values $\{v_i \in \mathbb{R}\}_{i=1}^Q$, which is given by:

$$a_q^{(w,h)} = v_k, \quad k = \arg \min_j \|a^{(w,h)} - v_j\|_2, \quad (9)$$

where $w = 1 \dots W_a, h = 1 \dots H_a$ are spatial indices. In this way, each score $a^{(w,h)}$ in the continuous attention map is mapped to the 1-of- Q anchor value. The quantized attention map a_q and the input x are then encoded into a latent representation $z \in \mathbb{R}^K$, where K is the dimension of the latent space. Finally, z is mapped to the prediction probabilities $y \in \mathbb{R}^C$, and C is the number of classes. The complete model parameters include the parameters of the attention module, encoder, decoder, and the anchor values $\{v_i \in \mathbb{R}\}_{i=1}^Q$.

As the $\arg \min$ operation in Eq. (9) is not differentiable, we resort to the straight-through estimator [Bengio *et al.*, 2013]

and approximate the gradient of a_q using the gradients of a . Though simple, this estimator worked well for the experiments in this paper. To be concrete, in the forward process the quantized attention map a_q is passed to the encoder, and during the backwards computation, the gradient of a is passed to the attention module unaltered. Such a gradient approximation makes sense because a_q and a share the same $W_a \times H_a$ dimensional space, and the gradient of a can provide useful information on how the attention module could change its output to minimize the loss function defined in Eq. (8).

The overall loss function is thus defined as in Eq. (10), which extends Eq. (8) with two terms, namely a quantization objective $\|\text{sg}[g(x_n, \varepsilon)] - a_q^\varepsilon\|_2^2$ weighted by λ_q , and a commitment term $\|g(x_n, \varepsilon) - \text{sg}[a_q^\varepsilon]\|_2^2$ weighted by λ_c , where $\text{sg}[\cdot]$ is the stopgradient operator [Van Den Oord *et al.*, 2017], and a_q^ε is the quantized version of $a = g(x_n, \varepsilon)$. The former updates the anchor values to move towards the attention map a , and the latter forces the attention module to commit to the anchor values. We set $\beta = 0.01$, $\lambda_q = 0.4$, and $\lambda_c = 0.1$ empirically.

$$\begin{aligned} \mathcal{L} = & -\frac{1}{N} \sum_{n=1}^N \{ \mathbb{E}_{\varepsilon \sim p(\varepsilon)} [\mathbb{E}_{\epsilon \sim p(\epsilon)} [\log q(y_n | f(x_n, a_q^\varepsilon, \epsilon))]] \\ & + \mathbb{E}_{\varepsilon \sim p(\varepsilon)} [\beta D_{\text{KL}} [p(z|x_n, a_q^\varepsilon) \parallel r(z)] \\ & + \lambda_q \|\text{sg}[g(x_n, \varepsilon)] - a_q^\varepsilon\|_2^2 + \lambda_c \|g(x_n, \varepsilon) - \text{sg}[a_q^\varepsilon]\|_2^2 \}. \end{aligned} \quad (10)$$

An illustration of the whole framework is shown in Fig. 2. In practice, we first use an feature extractor, *e.g.* VGGNet [Simonyan and Zisserman, 2015], to extract an intermediate feature f from the input x , then learn the attention a, a_q and the variational encoding z from f instead of x .

4 Experiments

To demonstrate the effectiveness of the proposed IB-inspired spatial attention, we conduct extensive experiments on various visual recognition tasks, including image classification (§4.1), fine-grained recognition (§4.2), and cross-dataset classification (§4.3), and achieve improved performance over baseline models. In §4.4, we compare the interpretability of our attention maps with those of other attention models both qualitatively and quantitatively. We conduct an ablation study in §4.5. More details are shown in the supplementary.

4.1 Image Classification

Datasets and models. *CIFAR-10* [Krizhevsky *et al.*, 2009] contains 60,000 32×32 natural images of 10 classes, which are split into 50,000 training and 10,000 test images. *CIFAR-100* [Krizhevsky *et al.*, 2009] is similar to *CIFAR-10*, except that it has 100 classes. We extend standard architectures, VGG and wide residual network (WRN), with the proposed IB-inspired spatial attention, and train the whole framework from scratch on *CIFAR-10*, and *CIFAR-100*, respectively. We use original input images after data augmentation (random flipping and cropping with a padding of 4 pixels).

Results on CIFAR. As shown in Table 1, the proposed attention mechanism achieves noticeable performance improvement over standard architectures and existing attention mech-

Model	Image Class.		Fine-grained Recog.		Cross-domain Class.	
	CIFAR-10	CIFAR-100	CUB-200-2011	SVHN	STL10-train	STL10-test
– Existing architectures –						
VGG [Simonyan and Zisserman, 2015]	7.77	30.62	34.64	4.27	54.66	55.09
VGG-GAP [Zhou <i>et al.</i> , 2016]	9.87	31.77	29.50	5.84	56.76	57.24
VGG-PAN [Seo <i>et al.</i> , 2018]	6.29	24.35	31.46	8.02	52.50	52.79
VGG-DVIB [Alemi <i>et al.</i> , 2017]	4.64*	22.88*	23.94*	3.28*	51.40*	51.60*
WRN [Zagoruyko and Komodakis, 2016]	4.00	19.25	26.50	–	–	–
– Architectures with attention –						
VGG-att2 [Jetley <i>et al.</i> , 2018]	5.23	23.19	26.80	3.74	51.24	51.71
VGG-att3 [Jetley <i>et al.</i> , 2018]	6.34	22.97	26.95	3.52	51.58	51.68
WRN-ABN [Fukui <i>et al.</i> , 2019]	3.92*	18.12	–	2.88*	50.90*	51.24*
VGG-aib (ours)	4.28	21.56	23.73	3.24	50.64	51.24
VGG-aib-qt (ours)	4.10	20.87	21.83	3.07	50.44	51.16
WRN-aib (ours)	3.60	17.82	17.26	2.76	50.08	50.84
WRN-aib-qt (ours)	3.43	17.64	15.50	2.69	50.34	50.49

Table 1: Top-1 error for image classification (§4.1), fine-grained recognition (§4.2), and cross-dataset classification (§4.3). * denotes re-implementation or re-training. Other values are from the original paper. Best values of different backbones are in **bold**.

Model	Spatial	CIFAR-10				CIFAR-100				Frequency	CIFAR-10	CIFAR-100
		$p=4$	$p=8$	$p=12$	$p=16$	$p=4$	$p=8$	$p=12$	$p=16$			
VGG-att3*	color	91.46	79.61	37.71	7.12	52.92	39.93	25.40	14.56	$r > 4$	83.06	3.69
	svhn	90.97	75.70	36.74	6.51	82.08	63.16	39.07	21.03	$r < 12$	49.61	50.90
VGG-aib	color	99.22	99.69	93.78	20.59	98.88	98.56	95.92	22.70	$r > 4$	99.91	99.78
	svhn	98.59	97.52	97.35	72.86	98.73	96.70	96.69	93.02	$r < 12$	53.26	79.13
VGG-aib-qt	color	99.26	99.79	91.10	18.36	99.18	99.30	94.59	20.54	$r > 4$	99.96	99.60
	svhn	98.65	98.04	97.85	78.82	99.12	97.64	97.21	94.79	$r < 12$	73.52	79.70
WRN-ABN	color	90.76	65.01	33.89	13.24	89.74	61.38	30.56	9.67	$r > 4$	38.14	14.04
	svhn	90.40	68.41	38.46	16.55	92.77	63.67	30.57	9.47	$r < 12$	36.33	25.43
WRN-aib	color	99.95	93.94	45.17	6.69	99.86	95.35	64.27	17.15	$r > 4$	78.96	90.44
	svhn	99.94	97.34	81.98	47.65	99.90	97.77	89.37	62.64	$r < 12$	84.58	94.18
WRN-aib-qt	color	99.84	84.18	28.94	4.64	99.97	97.07	69.51	25.80	$r > 4$	72.05	94.13
	svhn	99.91	96.05	70.75	28.35	99.95	98.52	89.00	63.10	$r < 12$	76.53	93.17

Table 2: Interpretability scores under spatial and frequency domain modification on CIFAR-10 and CIFAR-100. p is the window size of the modified region. r is the radius in frequency domain. See §4.4 for more details. * denotes re-implementation. Best values in **bold**.

anisms such as GAP, PAN, *VGG-att*¹ and ABN². To be specific, *VGG-aib* achieves 3.49% and 9.06% decrease of errors over the baseline VGG model on CIFAR-10 and CIFAR-100, respectively. The quantized attention model *VGG-aib-qt* further decreases the errors over *VGG-aib* by 0.18% and 0.69% on the two datasets. Compared with other VGG-backed attention mechanisms, ours also achieve superior classification performances. Similarly, *WRN-aib* and *WRN-aib-qt* also decrease the top-1 errors on CIFAR-10 and CIFAR-100.

4.2 Fine-grained Recognition

Datasets and models. *CUB-200-2011* (CUB) [Wah *et al.*, 2011] contains 5,994 training and 5,794 testing bird images from 200 classes. *SVHN* collects 73,257 training, 26,032 testing, and 531,131 extra digit images from house numbers in street view images. For CUB, we perform the same pre-processing as [Jetley *et al.*, 2018]. For SVHN, we apply the same data augmentation as CIFAR.

Results on CUB. The proposed *VGG-aib* and *VGG-aib-qt* achieves smaller classification error compared with baselines built on VGG, including GAP, PAN, and *VGG-att*. Specially, *VGG-aib* and *VGG-aib-qt* outperform *VGG-att* for a 3.07%

and 4.97%, respectively.

Results on SVHN. Our proposed method achieves lower errors with VGG-backed models, and comparative errors for WRN backbone methods.

4.3 Cross-domain Classification

Datasets and models. *STL-10* contains 5,000 training and 8,000 test images of resolution 96×96 organized into 10 classes. Following [Jetley *et al.*, 2018], the models trained on CIFAR-10 are directly tested on STL-10 training and test sets without finetuning to verify the generalization abilities.

Results on STL-10. As shown in Table 1, the proposed attention model outperforms other competitors on VGG backbone, and achieves comparative performance for WRN backbone.

4.4 Interpretability Analysis

An *interpretable* attention map is expected to faithfully highlight the regions responsible for the model decision. Thus, an *interpretable* attention mechanism is expected to yield consistent attention maps for an original input and a modified input if the modification does not alter the model decision. Here, we quantify the interpretability of an attention mechanism by calculating the ‘interpretability score’, *i.e.* the percentage of attention-consistent samples in prediction-consistent samples under modifications in the spatial or frequency domain. Here,

¹ <https://github.com/SaoYan/LearnToPayAttention>

² https://github.com/machine-perception-robotics-group/attention_branch_network

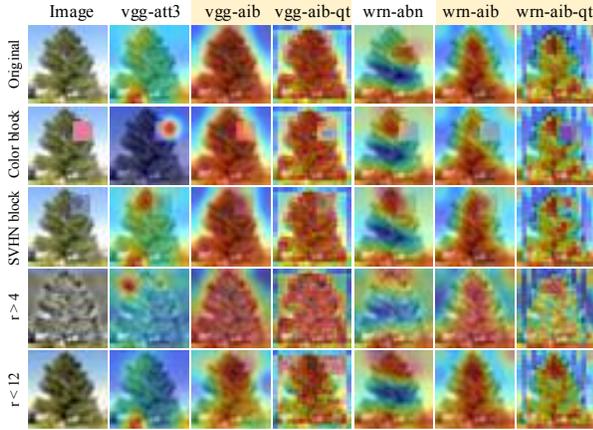


Figure 3: Visualization of attention maps for interpretability (§4.4).

the attention consistency is measured by the cosine similarity between two flattened and normalized attention maps.

The *spatial domain modification* includes randomly occluding the original images in CIFARs with color blocks or images drawn from distinct datasets. The size of the modified region p ranges from 4 to 16. The 2nd and 3rd rows in Fig. 3 show exemplar images occluded by a random color block and an image randomly drawn from SVHN, respectively, where $p = 8$. As can be observed, our spatial attention model *VGG-aib(-qt)*, and *WRN-aib(-qt)* yield consistent attention maps with the original images (first row). The interpretability scores are listed in Table 2. Our method consistently outperforms other spatial attention mechanisms with the same backbone by a large margin on two datasets for various p . This is because the IB-inspired attention mechanism minimizes the MI between the attention-modulated features and the inputs, thus mitigating the influence of ambiguous information exerted on the inputs to some extent.

We also conduct *frequency domain modification*, which is done by performing Fourier transform on the original samples, and feeding only high-/low-frequency (HF/LF) components into the model. To preserve enough information and maintain the classification performance, we focus on HF components of $r > 4$, and LF components of $r < 12$, where r is the radius in frequency domain defined as in [Wang *et al.*, 2020]. The 4th and 5th rows in Fig. 3 show exemplar images constructed from HF and LF components, respectively. Our attention maps are more royal to those of the original images compared with other competitors. Our method also yields much better quantitative results than other attention models, as illustrated in Table 2. This is because our IB-inspired attention mechanism can well capture the task-specific information in the input by maximizing the MI between the attention-modulated feature and the task output, even when part of the input information is missing.

4.5 Ablation Study

We conduct ablation studies on *CIFAR-10* with the VGG backbone to assess the effectiveness of each component.

Effectiveness of attention module. Table 1 shows that *VGG-aib* and *VGG-aib-qt* outperform the IB-based representation

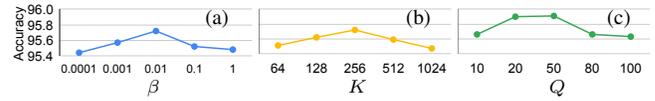


Figure 4: Ablation study on CIFAR-10 with VGG backbone (§4.5).

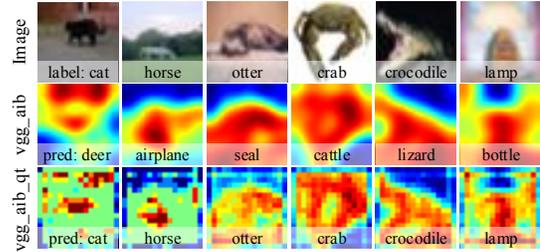


Figure 5: Effect of attention score quantization. See §4.5 for details.

learning model *VGG-DVIB*.

Information tradeoff. β controls the amount of information flow that bypasses the bottleneck of the network. To measure the influence of β on the performance, we plot the accuracy values with varying β in Fig. 4 (a). As can be observed, the accuracy is largest when $\beta = 0.01$.

Latent vector dimension. We experiment on $K = 64, 128, 256, 512, 1024$. As shown in Fig. 4 (b), $K = 256$ achieves the best performance.

Attention score quantization. Fig. 4 (c) shows the classification accuracy when varying number of anchor values Q , where Q between 20 and 50 gives better performance. Exemplary attention maps of cases that are wrongly classified by *VGG-aib* but are correctly predicted by *VGG-aib-qt* are listed in Fig. 5. As can be observed, attention quantization can further help focus on more concentrated regions with important information, thus improve the prediction accuracy.

5 Conclusion

We propose a spatial attention mechanism based on IB theory for generating probabilistic maps that minimizes the MI between the masked representation and the input, while maximizing the MI between the masked representation and the task label. To further restrict the information bypassed by the attention map, we incorporate an adaptive quantization mechanism to regularize the attention scores by rounding the continuous scores to the nearest anchor value during training. Extensive experiments show that the proposed IB-inspired spatial attention mechanism significantly improves the performance for visual recognition tasks by focusing on the most informative parts of the input. The generated attention maps are interpretable for the decision making of the DNNs, as they consistently highlight the informative regions for the original and modified inputs with the same semantics.

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