DaringFed: A Dynamic Bayesian Persuasion Pricing for Online Federated Learning Under Two-sided Incomplete Information*

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Abstract

Online Federated Learning (OFL) is a real-time learning paradigm that sequentially executes parameter aggregation immediately for each random arriving client. To motivate clients to participate in OFL, it is crucial to offer appropriate incentives to offset the training resource consump-However, the design of incentive mechanisms in OFL is constrained by the dynamic variability of Two-sided Incomplete Information (TII) concerning resources, where the server is unaware of the clients' dynamically changing computational resources, while clients lack knowledge of the real-time communication resources allocated by the server. To incentivize clients to participate in training by offering dynamic rewards to each arriving client, we design a novel Dynamic Bayesian persuasion pricing for online Federated learning (DaringFed) under TII. Specifically, we begin by formulating the interaction between the server and clients as a dynamic signaling and pricing allocation problem within a Bayesian persuasion game, and then demonstrate the existence of a unique Bayesian persuasion Nash equilibrium. By deriving the optimal design of DaringFed under one-sided incomplete information, we further analyze the approximate optimal design of DaringFed with a specific bound under TII. Finally, extensive evaluation conducted on real datasets demonstrate that DaringFed optimizes accuracy and converges speed by 16.99\%, while experiments with synthetic datasets validate the convergence of estimate unknown values and the effectiveness of DaringFed in improving the server's utility by up to 12.6%.

1 Introduction

Online Federated Learning (OFL) extends Federated Learning (FL) by allowing numerous clients to collaboratively train a global model in a sequential manner, enabling realtime model updates as a random client arrives [Chen et al., 2020]. The efficient leverage of computation and communication resources while ensuring data privacy, OFL is emerging as a crucial research direction [Xie et al., 2019; Dong et al., 2023]. Since training consumes clients' computation and communication resources, establishing an efficient compensation to encourage clients collaboration is a key issue for the success of OFL [Pang et al., 2023].

To address the challenges arising from dynamically varying resources and real-time reward allocation requirements in the context of incomplete information, it is crucial to focus on client incentive issues in OFL. Some literatures optimistically assume that the server is aware of all clients' local computation resources [Zhu et al., 2022; Li et al., 2022; Cui et al., 2023], or relaxes this assumption by assuming that the server is only aware of their distribution [Hu et al., 2022]. Other literatures hypothesize that the amount of communication resources is publicly available to clients [Zhang et al., 2023; Saha et al., 2022; Yuan et al., 2021]. In summary, existing literatures commonly make assumptions to mitigate the dynamic nature and incompleteness in OFL, which are difficult to hold in practical scenarios and hinder its sustainable development.

Given the factors mentioned, researching an efficient incentive mechanism in OFL is both urgent and challenging, especially under dynamically varying Two-sided Incomplete Information (TII), where both the server and clients possess constantly changing incomplete information about each other. First, clients lack knowledge of the dynamically varying available communication resources [Agrawal et al., 2024; Hu et al., 2022; Ding et al., 2020]. Due to dynamic network conditions and the server's privacy concerns, clients have only statistical information about the com-

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munication resources allocated by the server. In this context, the server strategically disclose partial information to each arriving client to influence their participation decisions and achieve favorable outcomes. However, ensuring clients trust the disclosed information and align their actions with the server's expectations remains challenging. Second, the real-time computation resources owned by the clients are unknown to the server [Deng et al., 2022; Li et al., 2021; Cho et al., 2020]. The distribution of clients' computation resources is difficult for the server to estimate and is influenced by dynamic changes due to factors such as varying geographical locations and fluctuating device battery levels over time. Without knowledge of this distribution, estimating it based on the constantly updated historical information as accurately as possible remains a challenge.

To overcome the abovementioned challenges, we design a novel Dynamic Bayesian persuasion pricing for online Federated learning under TII, named DaringFed, which aims to persuade clients to participate in training by strategically disclose its private available communication resources and offering dynamic rewards to each arriving client. Specifically, in the design of DaringFed, the Bayesian persuasion signal rule allows the server to modify the posterior distribution of communication resources on the client side, thereby maximizing the server's utility by persuading clients to make decisions that are favorable to the server. The dynamic pricing rule transforms the problem of lacking distribution knowledge of clients' local computation resources into a multiarmed bandit problem, and applies a confidence bound policy to estimate this distribution, thus dynamically incentivizing and filtering client participation in OFL. We summarize our main contributions as follows:

- Theoretically, to maximize the server's utility in OFL under TII, we incorporate Bayesian persuasion and dynamic pricing into the mechanism design. Bayesian persuasion influences clients' beliefs about communication resources and modify their participation decisions by sending signals from the server. Meanwhile, dynamic pricing adapts rewards based on historical client decision-making, without prior knowledge of the clients.
- Methodologically, we start by modeling the interaction between the server and clients as a Bayesian persuasion game within the TII context, and subsequently prove the existence of a unique Bayesian persuasion Nash equilibrium. Following this, we design an approximate optimal DaringFed mechanism to approximate the maximization of the server's utility. Finally, we prove that there exists a specific bound on the difference between the approximate optimal solution and the optimal one.
- Experimentally, extensive experiments conducted on real datasets show that DaringFed optimizes accuracy and converges speed by 16.99%. On synthetic datasets, we demonstrate that the approximate solution in DaringFed can converge, and the server's utility can be improved by up to 12.6% using the proposed mechanism.

2 Related Work

Incentive Mechanism for FL. Since clients are resourceconstrained and unwilling to participate in FL training, it is necessary to motivate and attract high-quality clients through a well-designed incentive mechanism [Wang et al., 2022]. For example, Cui et al. [2022] proposed an asynchronous FL scheme that sequentially selects clients and estimates the reward value by integrating cooperative game and the Shapley value. Ding et al. [2023] derived an optimal contract and pricing mechanism to address the dynamic asynchronous issue. The above works focus on optimizing FL performance through optimal scheme design or clients selection algorithm, but cannot be directly adapted to address the dynamic and incomplete information context in FL. Unlike the above studies, we discuss and derive an approximate optimal mechanism that not only improves the performance but also operates under the context of TII, making it applicable to real-world FL.

Incomplete Information in FL. In a realistic FL platform, the server and clients have limited information about each other in terms of available resources [Hu et al., 2022]. Some works had proposed practical scenarios for recovering this incomplete information. For instance, Ding et al. [2020] and Wang et al. [2022] designed the optimal contract in the presence of incomplete information about clients' type for the server. Hu et al. [2022] and Mingjun et al. [2023] modeled a Bayesian game to make resource or reward allocation decisions with incomplete information, where a client lacks personal information about others. Existing works are mainly concerned about one-sided incomplete information scenario, where the server is unaware of clients' inherent information, or clients' lack information about other clients or the server. However, a practical FL platform is a dynamic changing TII context, where not only the server unknown the clients' inherent dynamic computation resources, but also the clients are unaware of the server's real-time communication resources, which need to be allocated to those of the clients. To address this challenge, we model the Bayesian persuasion game and further analyze the optimal signal and payment rules in the proposed mechanism under context of TII in FL.

OFL. OFL performs model updates immediately upon a random client arrives [Chen *et al.*, 2020]. Most existing works in OFL focus on resource allocation and clients selection research. For instance, Chen *et al.*[2020] and Han *et al.*[2020] designed update strategies and adaptive gradient sparsification techniques to reduce resource consumption. Damaskinos *et al.*[2022] and Zhu *et al.*[2022] addressed the client selection through staleness awareness and performance prediction. Existing works overlook the resources dynamic and incomplete information in OFL, which may not applicable in practical scenarios and prevent its successful sustainable development. In contrast, we consider these context and design an incentive mechanism for a more general and practical scenario in OFL.

3 Problem Formulation

In this section, we introduce the system overview, pricing model, and formulate the server's cost minimization problem in OFL.

3.1 System Overview of OFL

In OFL, the global model is dynamically and sequentially updated in real-time based on clients' local training results. The OFL framework consists of a server and N clients, denoted by $\mathcal{N}=\{1,\cdots,N\}$, and operates over a series of time slots $\mathcal{T}=\{1,\cdots,T\}$. At each time slot $t\in\mathcal{T}$, a client $n_t\in\mathcal{N}$ arrives at the OFL platform and determines whether to join the training. We define ω_t and ω_t^n as the global model parameters and the local model parameters of client n_t respectively, and let x_n^t denotes the local training data of client n_t . If the arriving client n_t decides to participate in the FL training, she will perform her local update process as follows:

$$\omega_{t+1}^n = \omega_t^n - \eta \nabla l(\omega_t, x_t^n), \tag{1}$$

where η is the learning rate, and $\nabla l(\omega_t, x_t^n)$ is the gradient of local average loss $l(\omega_t, x_t^n)$.

After the client n_t finishes the local update, the server integrates the received update into the global model immediately, without waiting for all clients to complete their local computations and transmissions, i.e.,

$$\omega_{t+1} = (1 - \alpha)\omega_t + \alpha\omega_{t+1}^n, \tag{2}$$

where α is the weighting factor that controls the server's incorporation of the client's update into the global model.

3.2 Pricing Model

If the client n_t decides to join the FL training, her utility is the difference between the reward $\gamma_t \in [\gamma, \overline{\gamma}]$ offered by the server and the cost c_t incurred during model training. The cost c_t consists of computation and communication consumption [Huang et al., 2022]. Computation cost (measured by client CPU cycles and CPU frequency) for computing local gradients [Zhao et al., 2023]. Communication cost (measured by allocated bandwidth) for transmitting local gradients to the server [Zhang et al., 2023]. The client n_t with adequate computing resources can complete local training more efficiently by reducing computational delays and computation energy consumption. Then, the higher the computation resources $\theta_t \in [\theta, \overline{\theta}]$ that the client n_t has, the lower the computation cost. The client n_t with adequate communication resources can accelerate the upload of local gradients, reducing communication time and communication energy consumption [Hu et al., 2022]. Then, the higher the communication resources $\tau_t \in [\tau, \overline{\tau}]$ assigned by the server to the client n_t , the lower the communication cost. Therefore, the cost of client n_t is determined by the computation resources θ_t inherent to the client and the communication resources τ_t assigned by the server, i.e. $c_t(\theta_t, \tau_t)$. Note that the cost function $c_t(\theta_t, \tau_t)$ related to θ_t and τ_t is public knowledge for both the server and the clients. All clients have the same form of cost function. Therefore, we omit the subscript t for c_t , i.e., $c_t(\theta_t, \tau_t)$. Rational clients are willing to join FL if and only if the received reward exceeds the suffered cost $c(\theta_t, \tau_t)$, i.e. $\gamma_t \geq c(\theta_t, \tau_t)$.

One round of the OFL process can be detailed as follows: First, the server sends the latest reward γ_t and allocable available communication resources τ_t to the arriving client n_t (step ①). Second, the client estimates the cost $c(\theta_t, \tau_t)$ and determines whether to join the FL training process (step ②).

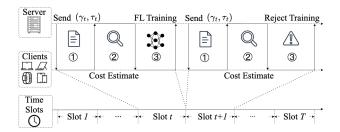


Figure 1: An overview of OFL.

If the client decides to engage in FL training, the server sends the latest global model parameters ω_t to the client, and the client sends back the updated local model parameters ω_{t+1}^n to the server after finishing local training. Otherwise, the server needs to wait for the next client arrive and participate in training (step 3). Finally, the server updates the global model ω_{t+1} according to Eq. (2) immediately.

3.3 Cost Minimization Problem

The OFL process terminates when the global model accuracy reaches a predefined threshold ε , supposed at the final time slot T [Pang et al., 2023]. Let $v_s(\varepsilon)$ represent the actual valuation the server receives with global accuracy ε . Then, the server's objective of maximizing its utility u_s can be formulated as follows:

$$\max_{(\gamma_t, \tau_t)} u_s = \max[v_s(\varepsilon) - c_s(\gamma_t, \tau_t)],$$
s.t. $c_s(\gamma_t, \tau_t) = \sum_{t=1}^T \mathbf{1}[\gamma_t \ge c(\theta_t, \tau_t)]\gamma_t,$
(3)

where $\mathbf{1}(\gamma_t \geq c(\theta_t, \tau_t))$ is an indicator function indicating whether client t joins the FL training. We declare that the reward given to clients here as the server's cost c_s , which the server needs to compensate for the clients' service.

Considering that the global accuracy ε is fixed, $v_s(\varepsilon)$ is constant and can therefore be ignored. Clients with lower computation resources will lead to training bias, effecting the model's generalization capability and causing overfitting issues. To prevent this issue, the server needs to filter clients whose computation resources θ_t are below the threshold β by adjusting the reward γ_t . Consequently, maximizing the server's utility can be reformulated as follows:

$$\min_{(\gamma_t, \tau_t)} c_s(\gamma_t, \tau_t),$$
s.t.
$$\begin{cases}
c_s(\gamma_t, \tau_t) = \sum_{t=1}^T \mathbf{1}[\gamma_t \ge c(\theta_t, \tau_t)] \gamma_t, \\
\min\{\theta_t | \gamma_t \ge c(\theta_t, \tau_t)\} \ge \beta.
\end{cases}$$
(4)

In the context of TII, it is difficult for the server to minimize the cost without having complete information about each client's decision to join the FL training. On the one hand, the communication resource τ_t assigned by the server to client t is confidential to the client. On the other hand, the computation resource θ_t inherent to client t is private information for the server. Therefore, it is challenging for a client to decide whether to participate in OFL training, and for the server to provide a suitable reward that ensures adequate clients join while minimizing the cost.

4 DaringFed Mechanism

In this section, we model the server's cost minimization problem in OFL under TII using the Bayesian persuasion game, and design a novel DaringFed mechanism to address it.

4.1 Bayesian Persuasion Game

The Bayesian persuasion (BP) game is a game-theoretic framework that investigates how the sender can strategically disclose private information through sending signals to persuade the receiver to make decisions favorable to the sender [Kamenica and Gentzkow, 2011]. Specifically, in this model, the server acts as a sender, sending signals, while the client acts as a receiver, receiving signals and making decision. Signals $\sigma \in \Sigma$ are sent to update the posterior distribution of communication resource. We assume that the computation resource θ_t and communication resource τ_t are i.i.d. across all clients, thus, we can omit subscript t for Eq. (4). Therefore, the Bayesian persuasion problem can be formulated as the expected server's cost for any client t, i.e.,

$$\arg \min_{(\gamma^*, \sigma^*)} c_s(\gamma, \sigma),$$
s.t.
$$\begin{cases} c_s(\gamma, \sigma) = \sum_{t=1}^T \mathbf{1}[\gamma \ge c(\theta, \sigma)]\gamma, \\ \min\{\theta | \gamma \ge c(\theta, \tau)\} \ge \beta, \end{cases}$$
(5)

where γ^* and σ^* represent the optimal reward and signal that minimize the server's cost, respectively.

4.2 Formalization of DaringFed Mechanism

DaringFed integrates a Bayesian persuasion signal rule to estimate the posterior expectation of the communication resources τ , and a dynamic pricing rule to determine the amount of reward γ in a TII environment.

Definition 1. (DaringFed) DaringFed mechanism is represented as a 2-tuple (\mathbb{S}, \mathbb{P}) , i.e., a Bayesian persuasion signal rule \mathbb{S} , and a dynamic pricing rule \mathbb{P} .

• S: $[\tau, \overline{\tau}] \times R^+ \to R^+$ determines how the distribution of the signal σ align with communication resources τ , i.e.,

$$\rho(\sigma|\tau) \leftarrow \frac{\phi(\tau|\sigma)}{\lambda(\tau)},\tag{6}$$

where $\phi(\cdot)$ is the Bayesian posterior distribution of τ after receiving signal σ , and $\lambda(\cdot)$ is the public prior distribution of τ .

• \mathbb{P} : $R^+ \times [\underline{\theta}, \overline{\theta}] \to R^+$ denotes the reward that the server can provide to a client, which is determined by the signal rule and the client's computation resources θ , i.e.,

$$\gamma \leftarrow \rho(\sigma|\tau)\theta. \tag{7}$$

We define μ as the posterior mean of τ , and transfer the Bayesian persuasion signal rule in DaringFed into selecting the distribution of μ over τ . And hence, Eq. (5) can be rewritten as the following optimization problem:

$$\arg \min_{(\gamma^*, \rho^*)} c_s(\gamma, \rho),
\text{s.t.} \begin{cases} c_s = \gamma \int_{\underline{\tau}}^{\overline{\tau}} \lambda(\tau) \int_{\underline{\tau}}^{\overline{\tau}} \rho(\mu | \tau) \psi(\gamma, \mu) d\mu d\tau, \\ \min\{\theta | \gamma \ge \int_{\underline{\tau}}^{\overline{\tau}} \lambda(\tau) \int_{\underline{\tau}}^{\overline{\tau}} \rho(\mu | \tau) c(\theta, \mu) d\mu d\tau\} \ge \beta, \end{cases}$$
(8)

where $\psi(\gamma,\mu)$ defines the probability that a client is willing to join FL training when the reward is γ and her posterior estimate of the communication resources is μ .

To ensure the posterior belief remains correct after being updated with prior public information and signals, the distribution of ρ is feasible if and only if it satisfies the Bayesian Consistency (BayesCon) [Agrawal *et al.*, 2024]. Additional, to guarantee the signals encourage clients to adjust their strategies in ways that benefit the server, while maintaining alignment between the clients' expected posterior belief and the prior, the distribution of ρ should also satisfy Bayesian Plausible (BayesPla) and Bayesian Benefit (BayesBen) [Kamenica and Gentzkow, 2011]. We provide formal definitions of BayesCon, BayesPla, and BayesBen as follows.

Definition 2. (BayesCon) ρ satisfies BayesCon if

$$\frac{\int_{\underline{\tau}}^{\overline{\tau}} \lambda(\tau) \rho(\mu|\tau) \tau d\tau}{\int_{\underline{\tau}}^{\overline{\tau}} \lambda(\tau) \rho(\mu|\tau) d\tau} = \mu. \tag{9}$$

Definition 3. (BayesPla) ρ satisfies BayesPla if

$$\int_{\underline{\tau}}^{\overline{\tau}} \lambda(\tau) \int_{\underline{\tau}}^{\overline{\tau}} \rho(\mu|\tau) \mu d\mu d\tau = \int_{\underline{\tau}}^{\overline{\tau}} \lambda(\tau) \tau d\tau.$$
 (10)

Definition 4. (BayesBen) ρ satisfies BayesBen if

$$\int_{\underline{\tau}}^{\overline{\tau}} \lambda(\tau) \int_{\underline{\tau}}^{\overline{\tau}} \rho(\mu|\tau) \psi(\gamma,\mu) d\mu d\tau \ge \int_{\underline{\tau}}^{\overline{\tau}} \lambda(\tau) \psi(\gamma,\tau) d\tau. \tag{11}$$

Therefore, the DaringFed mechanism design problem can be formulated as:

$$\arg \min_{(\gamma^*, \rho^*)} c_s(\gamma, \rho),$$

$$s.t. \begin{cases} c_s(\gamma, \rho) = \gamma \int_{\underline{\tau}}^{\overline{\tau}} \lambda(\tau) \int_{\underline{\tau}}^{\overline{\tau}} \rho(\mu | \tau) \psi(\gamma, \mu) d\mu d\tau, \\ \min\{\theta | \gamma \ge \int_{\underline{\tau}}^{\overline{\tau}} \lambda(\tau) \int_{\underline{\tau}}^{\overline{\tau}} \rho(\mu | \tau) c(\theta, \mu) d\mu d\tau\} \ge \beta, \\ \frac{\int_{\underline{\tau}}^{\overline{\tau}} \lambda(\tau) \rho(\mu | \tau) \tau d\tau}{\int_{\underline{\tau}}^{\overline{\tau}} \lambda(\tau) \rho(\mu | \tau) d\tau} = \mu, \\ \int_{\underline{\tau}}^{\overline{\tau}} \lambda(\tau) \int_{\underline{\tau}}^{\overline{\tau}} \rho(\mu | \tau) \mu d\mu d\tau = \int_{\underline{\tau}}^{\overline{\tau}} \lambda(\tau) \tau d\tau, \\ \int_{\underline{\tau}}^{\overline{\tau}} \lambda(\tau) \int_{\underline{\tau}}^{\overline{\tau}} \rho(\mu | \tau) \psi(\gamma, \mu) d\mu d\tau \ge \int_{\underline{\tau}}^{\overline{\tau}} \lambda(\tau) \psi(\gamma, \tau) d\tau. \end{cases}$$

DaringFed aims to minimize the server's cost, while ensuring clients' computation resources exceed a threshold, and satisfies BayesCon, BayesPla and BayesBen constraint under the optimal reward γ^* and signal ρ^* . Analyzing the existence of γ^* and ρ^* , and further identifying the optimal γ^* and ρ^* , constitutes the objective of DaringFed.

5 Design of DaringFed Mechanism

Due to the use of upper confidence bound for estimating the distribution of computation resources among clients, which involves a discrete decision space and limited exploration time, we can only derive an approximate optimal DaringFed. Consequently, in this section, we first analyze the existence of optimal DaringFed mechanism under one-sided incomplete information, where the server knows the distribution of computation resources among clients, and then design an approximately optimal DaringFed mechanism under a TII scenario.

Existence of Optimal DaringFed Mechanism

We define that θ follows a distribution with survival function $s(\theta)$, describing the probability that the computation resources exceed a threshold θ . Recall the indicator function $1(\gamma \geq c(\theta, \mu))$, which indicates whether a client decides to join the FL. The values of γ and μ determine the minimum threshold for a client's computation resources $\hat{\theta}$, i.e. $\hat{\theta} = \min\{\theta | \mathbf{1}(\gamma \geq c(\theta, \mu))\}$. If the client's computation resources θ exceeds this threshold $\hat{\theta}$, the client is willing to join FL. Following the survival distribution $s(\theta)$, the probability that a client's computation resources exceeds the threshold $\hat{\theta}$ is $s(\hat{\theta}) = s(\min\{\theta | \mathbf{1}(\gamma \geq c(\theta, \mu))\})$, which can be simplified as $s(\gamma, \mu)$. Therefore, we can reformulate Eq. (12) as:

$$\arg\min_{(\gamma^*, \rho^*)} c_s(\gamma, \rho)$$

$$\text{s.t.} \begin{cases} c_{s}(\gamma,\rho) = \gamma \int_{\underline{\tau}}^{\overline{\tau}} \lambda(\tau) \int_{\underline{\tau}}^{\overline{\tau}} \rho(\mu|\tau) s(\gamma,\mu) d\mu d\tau, \\ \min\{\theta|\gamma \geq \int_{\underline{\tau}}^{\overline{\tau}} \lambda(\tau) \int_{\underline{\tau}}^{\overline{\tau}} \rho(\mu|\tau) c(\theta,\mu) d\mu d\tau\} \geq \beta, \\ \frac{\int_{\underline{\tau}}^{\overline{\tau}} \lambda(\tau) \rho(\mu|\tau) \tau d\tau}{\int_{\underline{\tau}}^{\overline{\tau}} \lambda(\tau) \rho(\mu|\tau) d\tau} = \mu, \\ \int_{\underline{\tau}}^{\overline{\tau}} \lambda(\tau) \int_{\underline{\tau}}^{\overline{\tau}} \rho(\mu|\tau) \mu d\mu d\tau = \int_{\underline{\tau}}^{\overline{\tau}} \lambda(\tau) \tau d\tau, \\ \int_{\underline{\tau}}^{\overline{\tau}} \lambda(\tau) \int_{\underline{\tau}}^{\overline{\tau}} \rho(\mu|\tau) s(\gamma,\mu) d\mu d\tau \geq \int_{\underline{\tau}}^{\overline{\tau}} \lambda(\tau) s(\gamma,\tau) d\tau. \end{cases}$$

Our goal in designing DaringFed is to establish an ideal Bayesian persuasion Nash equilibrium (BPNE) when $s(\gamma, \mu)$ is known to the server, with the objective of maximizing the server's utility. To analyze the equilibrium of the BP game, we make the following common assumptions regarding the cost function $c(\theta, \tau)$ and survival function $s(\theta)$.

Assumption 1. The client's cost function $c(\theta, \tau)$ satisfies:

- Given any τ , the function $c(\theta, \tau)$ is a non-increasing, convex function w.r.t. θ .
- Given any θ , the function $c(\theta, \tau)$ is a non-increasing, convex function w.r.t. τ .

The assumption on the client's cost function are standard in many economics scenarios [Lu et al., 2023; Murhekar et al., 2024]. It is natural to assume that a client's cost decrease with its ability and the communication resource. The convexity of cost functions is commonly used to reflect increasing marginal costs.

Assumption 2. The survival function $s(\theta)$ is a nonincreasing, concave function w.r.t. θ .

The assumption regarding the survival function has ample justifications for it being a non-increasing, concave function [Hu et al., 2022; Bergstrom et al., 1986]. It is reasonable to assume that as the threshold value of θ increases, the number of clients who meet this criterion decreases, leading to a lower probability. The concave of the survival function is generally used to capture decreasing marginal probability.

In the BPNE, the server selects a distribution ρ and a reward γ that maximize its utility, as defined below.

Definition 5. (BPNE) Let (γ^*, ρ^*) denotes the BPNE, i.e.,

$$\begin{cases} c_s(\gamma^*, \rho^*) \ge c_s(\gamma^*, \rho), \\ c_s(\gamma^*, \rho^*) \ge c_s(\gamma, \rho^*). \end{cases}$$
(14)

At the BPNE, the server cannot benefit from changing its signals or rewards. Then, we investigate the existence and uniqueness of a BPNE.

Lemma 1. There exists a unique BPNE in the BP game.

Then, we derive the unique BPNE satisfying BayesCon, BayesPla, and BayesBen.

Theorem 1. The optimal signals ρ^* over posterior means μ *for the given prior value* $\tau \in [\underline{\tau}, \overline{\tau}]$ *are*

$$\begin{cases}
\rho(\mu|\underline{\tau}) = \frac{\rho(\mu)(\overline{\tau} - \mu)}{\lambda(\underline{\tau})(\overline{\tau} - \underline{\tau})}, \\
\rho(\mu|\overline{\tau}) = \frac{\rho(\mu)(\mu - \underline{\tau})}{\lambda(\overline{\tau})(\overline{\tau} - \underline{\tau})},
\end{cases}$$
(15)

where $\rho(\mu) = \frac{\lambda(\underline{\tau})\underline{\tau} + \lambda(\bar{\tau})\bar{\tau}}{\mu}$, and the optimal reward γ^* is $\arg\min\gamma\int_{\tau}^{\overline{\tau}}\rho(\mu)s(\gamma,\mu)d\mu.$

5.2 Approximate Optimal DaringFed Mechanism **Under TII**

In this section, we analyze the approximate optimal DaringFed mechanism in a TII scenario. Due to the uncertainty of $s(\gamma, \mu)$, the server needs to estimate it with respect to γ and μ first, and then design the optimal signal ρ and γ to maximize its expected utility.

To estimate $s(\cdot)$, we considering the reward space and the computation resources space are discrete spaces, i.e., $\gamma \in R$ and $\theta \in \Theta$, where $R = \{\underline{\gamma}, \underline{\gamma} + \xi, \cdots, \overline{\gamma} - \xi, \overline{\gamma}\}$ and $\Theta = \{\underline{\theta}, \underline{\theta} + \xi, \cdots, \overline{\theta} - \xi, \overline{\theta}\}$. Let $\mathcal{N}_t(\hat{\theta})$ represents the set of time rounds prior to time slot t where the threshold equals $\hat{\theta}$, i.e., $\mathcal{N}_t(\hat{\theta}) = \{n | (n \leq t) \cap (\hat{\theta} = \min\{\theta | \mathbf{1}(\gamma \geq t) \}) \}$ $c(\theta,\mu)$)}). $N_t(\hat{\theta})$ denote the total number of such time slots, i.e., $N_t(\hat{\theta}) = |\mathcal{N}_t(\hat{\theta})|$. Then, we can derive $\bar{s}(\hat{\theta})$ as follows.

Lemma 2. The upper confidence bound for the probability that the computation resources threshold is exactly θ is:

$$\overline{s}(\hat{\theta}) = \frac{\sum_{n \in \mathcal{N}_t(\hat{\theta})} \mathbf{1}(\gamma_n \ge c(\theta_n, \mu_n))}{N_t(\hat{\theta})} + \sqrt{\frac{\ln N}{2N_t(\hat{\theta})}}.$$
 (16)

We define the approximate optimal reward as $\gamma^+ \in R$, and the corresponding threshold for clients' computation resources as $\hat{\theta}^+ = \min\{\theta | \mathbf{1}(\gamma^+ \geq c(\theta, \mu))\}$. There exists $z \in \mathbb{Z}$ such that $(z-1)\xi \leq \hat{\theta}^+ \leq z\xi$ for $\theta \in \Theta$. Then, we can find two posterior expectation of communication resources, μ_r and μ_l , such that $(z-1)\xi = \min\{\theta | \mathbf{1}(\gamma^+ \geq c(\theta, \mu_r))\}\)$ and $z\xi = \min\{\theta | \mathbf{1}(\gamma^+ \geq c(\theta, \mu_l))\}$). In the following, we derive the approximate optimal signals ρ^+ from a given approximate optimal reward $\gamma^+ \in R$ using Theorem 2, and then design Algorithm 1 to obtain both γ^+ and ρ^+ globally.

Theorem 2. The approximate optimal signals ρ^+ that ensures the clients' computation resources threshold $\hat{\theta}$ exactly at the discrete space Θ are

$$\begin{cases} \rho^{+}(\mu_{l}|\underline{\tau}) = \frac{\rho(\mu_{l})(\overline{\tau} - \mu_{l})}{\lambda(\underline{\tau})(\overline{\tau} - \underline{\tau})}, \\ \rho^{+}(\mu_{l}|\overline{\tau}) = \frac{\rho(\mu_{l})(\mu_{l} - \underline{\tau})}{\lambda(\overline{\tau})(\overline{\tau} - \underline{\tau})}, \\ \rho^{+}(\mu_{r}|\underline{\tau}) = \frac{\rho(\mu_{r})(\overline{\tau} - \mu_{r})}{\lambda(\underline{\tau})(\overline{\tau} - \underline{\tau})}, \\ \rho^{+}(\mu_{r}|\overline{\tau}) = \frac{\rho(\mu_{r})(\mu_{r} - \underline{\tau})}{\lambda(\overline{\tau})(\overline{\tau} - \underline{\tau})}, \end{cases}$$

$$where \ \rho(\mu_{l}) = \frac{\rho(\mu)(\mu_{r} - \mu)}{\mu_{r} - \mu_{l}}, \ and \ \rho(\mu_{r}) = \frac{\rho(\mu)(\mu - \mu_{l})}{\mu_{r} - \mu_{l}}.$$

where
$$\rho(\mu_l) = \frac{\rho(\mu_l)(\mu_r - \mu)}{\mu_r - \mu_l}$$
, and $\rho(\mu_r) = \frac{\rho(\mu_l)(\mu - \mu_l)}{\mu_r - \mu_l}$.

Algorithm 1: Approximate Optimal Design of DaringFed

```
Input: \xi, \Theta = \{\underline{\theta}, \underline{\theta} + \xi, \cdots, \overline{\theta} - \xi, \overline{\theta}\},\ R = \{\underline{\gamma}, \underline{\gamma} + \xi, \cdots, \overline{\gamma} - \xi, \overline{\gamma}\}, \underline{\tau}, \overline{\tau}, \tau;
     Output: \rho, \gamma;
_{\mathbf{1}} for t\in\{1,2,\cdots,|\Theta|\} do
            \theta \leftarrow \underline{\theta} + t(\xi - 1);
        \gamma \leftarrow \{\theta = \min\{\theta | \mathbf{1}(\gamma \ge c(\theta, \tau))\}\};
4 for t = |\Theta| + 1; t < T; t + + do
             Traverse \theta \in \Theta to update s(\theta) by Eq. (16);
5
              for \gamma \in R do
6
                     z \leftarrow \{z | z \in \mathbb{Z}^+\} \cap \{(z-1)\xi \le \theta \le z\xi\};
 7
                     \mu_r \leftarrow \{(z-1)\xi = \min\{\theta | \mathbf{1}(\gamma \ge c(\theta, \mu_r))\}\};
 8
                      \mu_l \leftarrow \{z\xi = \min\{\theta | \mathbf{1}(\gamma \ge c(\theta, \mu_l))\}\};
                     Obtain \rho(\mu_l|\underline{\tau}), \rho(\mu_l|\overline{\tau}), \rho(\mu_r|\underline{\tau}), and \rho(\mu_r|\overline{\tau})
10
                        by Eq. (17);
                      Obtain c_s by Eq. (13);
11
                      Retain \gamma and \rho that minimizes c_s.
12
```

In Algorithm 1, to initialize $s(\theta)$, we traverse each element $\theta \in \Theta$ where $\theta = \hat{\theta}$, without any signaling mechanism, i.e., the posterior expectation of communication resources μ is equal to real value τ directly (lines 1-3). Then, for each arriving client, we update $s(\theta)$ based on the historically information, where the provided reward γ and signals ρ can persuasion clients to participate in FL training (line 5). Finally, we traverse $\gamma \in R$ to find the suitable γ and corresponding ρ according to Theorem 2, in order to minimize the server's cost c_s (lines 6-12). The retained γ and ρ represent the selected reward and signals for the current time slot, and this process can iterate continuously until γ convergence to γ^+ , or the distribution of clients' local computation resources changes.

In the TII scenario, the approximate optimal signals ρ and reward γ can only be obtained from the discrete space Θ and R, respectively. However, the optimal value may not lie within these discrete spaces. Here, we analyze the bounds on the approximate optimal value as follows.

Theorem 3. The bound on the approximate optimal value is

$$c_s(\gamma^+, \rho^+) - c_s(\gamma^*, \rho^*) \le 2\xi.$$
 (18)

According to Theorem 3, the approximate optimal solution obtained by Algorithm 1 in the TII almost converges to the optimal solution, with the gap bounded by 2ξ .

6 Experiments

In this section, we utilize four real datasets to evaluate the performance of the DaringFed under varying level of computation resources θ and communication resources τ . Subsequently, we employ a synthetic dataset to demonstrate the effectiveness of the DaringFed in terms of the convergence of the computation resources threshold $\hat{\theta}$ and the reward γ . Furthermore, we compare the improvements achieved by the DaringFed with non-DaringFed in relation to the computation resources threshold $\hat{\theta}$ and server's cost c_s .

Setup on real datasets. We estimate the performance of the DaringFed on four real-world datasets: MNIST [Yann et al., 2021], Fashion-MNIST [Xiao et al., 2017], FEMNIST [Caldas et al., 2018], and CIFAR-10 [Krizhevsky, 2009]. For MNIST and Fashion-MNIST, we employ a 4-layer convolutional neural network (CNN) model consisting of two 5×5 convolutional layers with 10 and 20 channels, respectively. For FEMNIST, we employ a 3-layer CNN model, consisting of a 7×7 convolutional layer with 32 channels, a 3×3 convolution layer with 64 channels, and a fully connected layer. For CIFAR-10, we employ a 5-layer CNN model consisting of two 5×5 convolution layers, each with 64 channels, followed by ReLU activation and 3×3 max pooling, and three fully connected layers. All of the above models are trained for 2000 time slots. Note that in the OFL platform, only one client arrives per time slot.

Setup on synthetic datasets. We analyze the impact of convergence on $\hat{\theta}$ and γ , as well as the improvements in $\hat{\theta}$ and c_s using a synthetic dataset. We generate τ from a uniform distribution over the interval [0.1,0.9]. We define $c=(1-\theta)^2(1.2-\mu)^2$, which satisfies Assumption 1, where $\mu,\theta\in[0.1,0.9]$. Additionally, we define $s(\theta)=1-(\frac{\theta-0.1}{0.8})^8$, where $\theta\in[0.1,0.9]$, to satisfy Assumption 2. For the discrete space in a TII scenario, we specific ξ as 0.01.

Performance of DaringFed. To the best of our knowledge, DaringFed represents the initial effort in designing an incentive mechanism for OFL under TII. To showcase the effectiveness of DaringFed (DF), we conduct a comparative analysis with its variants against a range of baselines to access the influence of different components within our proposed mechanism: (1) DaringFed (DF-B): without the Bayesian persuasion signal rule, where clients can only estimate communication resources based on the prior distribution. (2) DaringFed (DF-D): without the dynamic pricing rule, where the server provides clients with a fixed reward. (3) DaringFed (DF-BD): without both above rules.

Figure 2 illustrates the model accuracy versus time slot for different baselines. DaringFed achieves the highest accuracy and converges the fastest as shown in Table 1. DF-B and DF-D exhibit lower accuracy and slower convergence, while DF-BD has the worst accuracy and the slowest convergence. This demonstrates that DaringFed improves model performance by filtering out clients with low computation or communication resources in OFL. This is because only clients with sufficient computation or communication resources can meet the constraint that the cost is less than reward under a specific reward threshold, enabling their participation in OFL training. Allocating an appropriate reward through DaringFed, based on the distribution of clients' resources, can improve system performance. Even though clients resources change dynamically, DaringFed can adjust the reward based on feedback regarding whether each client join FL during per time slot.

Impact of Convergence on $\hat{\theta}$ and γ . Figure 3 (a) and (b) show that the client's local computation resource threshold $\hat{\theta}$ and reward γ can converge after numerous time slot iterations. Each time slot has an optimal computation resource threshold $\hat{\theta}^*$, which is determined by the arriving client's θ .

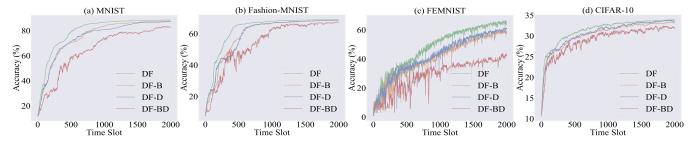


Figure 2: Testing the accuracy of OFL with the proposed DaringFed on (a) MNIST, (b) Fashion-MNIST, (c) FEMNIST, and (d) CIFAR-10.

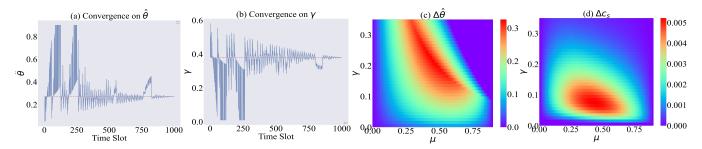


Figure 3: Convergence on (a) $\hat{\theta}$ and (b) γ ; Improvements on (c) $\hat{\theta}$ and (d) c_s .

| Datasets | Accuracy (%) | | | |
|---|----------------------------------|----------------------------------|----------------------------------|----------------------------------|
| | DF | DF-B | DF-D | DF-BD |
| MNIST Fashion-MNIST FEMNIST CIFAR-10 | 88.38 69.11 64.41 34.73 | 87.56 68.65 57.41 34.27 | 86.93 68.14 60.35 34.48 | 83.35 67.18 43.05 31.73 |

Table 1: Accuracy among different thresholds.

The optimal threshold $\hat{\theta}^*$ ensures reward equal to client's cost exactly, thereby maximizing the server's utility. However, $\hat{\theta}^*$ is unknown to the server, as the server is unaware of the distribution of the client's computation resource. There are multiple discrete values of $\hat{\theta}$ for the server to select from. The server needs to evaluate $\hat{\theta}$ by exploiting the available known knowledge that the selected $\hat{\theta}$ can persuade clients to join FL training, and by exploring the unknown knowledge regarding the unselected $\hat{\theta}$, which has never been chosen before. The server can estimate the distribution of θ through above process, and further converge to $\hat{\theta}^*$ and γ^* . This mechanism is still applicable in scenarios where the distribution of clients' computation resources is dynamic changing. After the distribution of clients' computation resources changes, the convergence value may changed after training, and multiple different convergence values can exist depending on distribution.

Improvements in $\hat{\theta}$ and c_s . Figure 3 (c) and (d) use heatmaps to evaluate the improvement in $\hat{\theta}$ and c_s from DF-BD to DaringFed across various values of μ and γ in OFL, i.e. $\Delta \hat{\theta} = \hat{\theta}^* - \hat{\theta}'$ and $\Delta c_s = c_s^* - c_s'$, where \cdot^* and \cdot' represents the results derived from DaringFed and DF-BD, respectively.

As shown in Figure 3 (c), $\Delta \hat{\theta}$ attains its maximum value for specific values of γ and μ . On the one hand, a higher μ reduce clients' cost, leading to lower values of $\hat{\theta}^{bp}$ and $\hat{\theta}^{non-bp}$ under a fixed γ . Since the function of $\hat{\theta}$ is a convex function according to Appendix A, when the posterior expectation of μ is fixed to satisfy Bayesian Plausible, there exists a maximum value of $\Delta \hat{\theta}$, and $\hat{\theta}^{bp}$ is greater than $\hat{\theta}^{non-bp}$, filter better clients under DaringFed. On the other hand, a higher γ reduce clients' cost, leading to lower values of $\hat{\theta}^{bp}$ and $\hat{\theta}^{non-bp}$ under a fixed μ . $\Delta \hat{\theta}$ reaches its maximum value when γ at the optimal value. As shown in Figure 3 (d), Δc_s attains its maximum value for specific values of γ and μ . On the one hand, the function of c_s is a concave according to Appendix A, under a fixed γ . There exists a maximum value for Δc_s when posterior expectation of μ is fixed to satisfy Bayesian Plausible, and c_s^{non-bp} is worse than c_s^{bp} . On the other hand, a higher γ leads to higher values of c_s^{bp} and c_s^{non-bp} under a fixed μ . And Δc_s reach a maximum value when γ is optimal.

7 Conclusion

In this paper, DaringFed was proposed to address the context of TII in the OFL platform, which integrated a Bayesian persuasion signal rule and a dynamic pricing rule. To overcome the challenge that clients' were unaware of the communication resources allocated by the server, a Bayesian persuasion signal rule was used to estimate the posterior expectation of communication resources on the clients' side. To tackle the challenge that the server was unaware of clients' inherent computation resources, a dynamic pricing rule was designed to incentive clients to participate in OFL under TII as much as possible to maximize the server's utility. Finally, extensive experiments were conducted on real and synthetic dataset to validate the effectiveness of DaringFed mechanism.

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